

# Replication

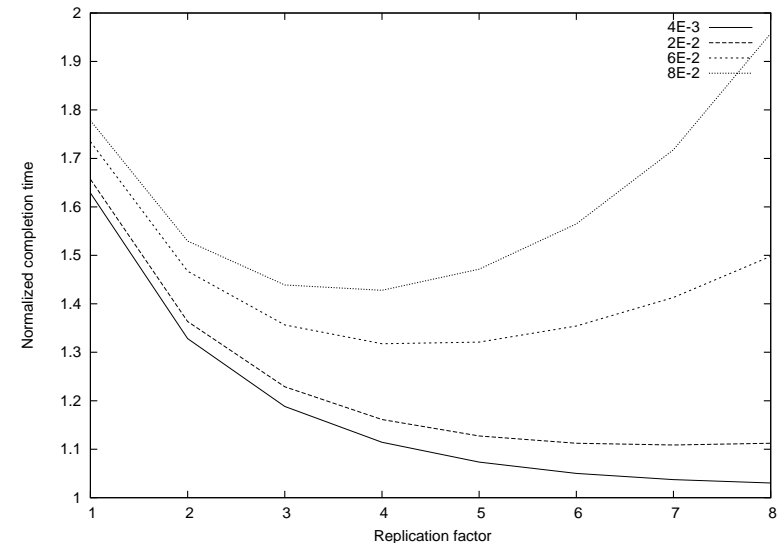
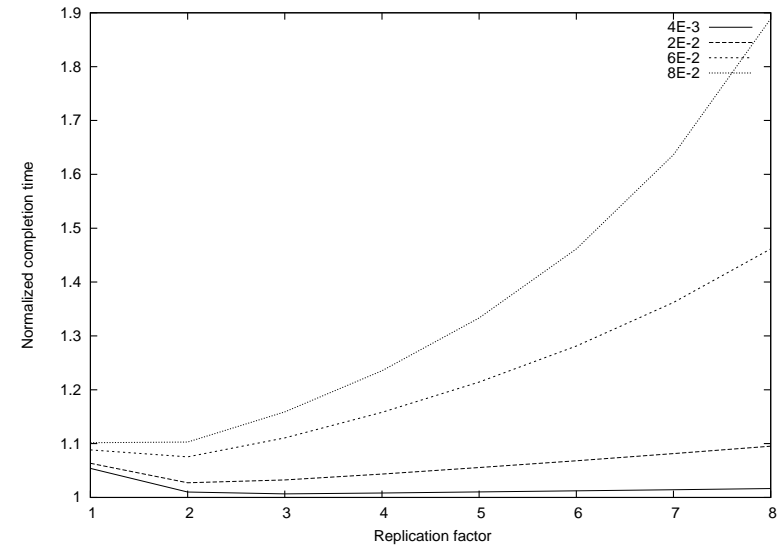
- Experimental study in [Kondo et al. 2002]
- Replication factor  $n$ , no keepalive, synchronous

$$\overline{T}_n = \frac{1}{\lambda(1 - (1 - e^{-\lambda})^n)} \sum_{k=1}^n \frac{(1 - e^{-\lambda})^k}{k}$$

- Infinite resource : the optimal latency can be closely approximated

$$\lim_{n \rightarrow \infty} \overline{T}_n = 1$$

- Completion time
  - M/G/1 queue, service time  $\overline{T}_n$
  - $n = 2$  or  $3$  is a reasonable tradeoff



# The Cost Model

- A job is falsified with **unknown** probability  $p$  - the defect rate
- $p_a$  the acceptable defect rate
- Non-productive system,  $p \geq p_a$  : the cost is the number of calls to the oracle  $s(p)$
- Productive system,  $p < p_a$  : the cost is number of calls to the oracle plus erroneous rejections

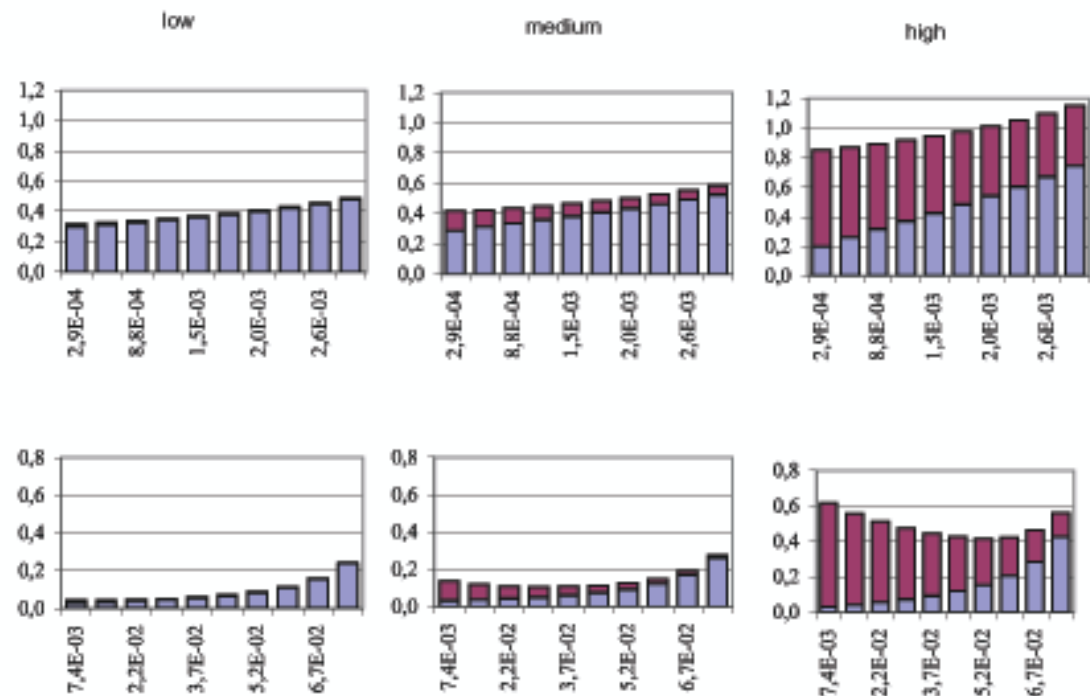
$$C(p) = \frac{1}{B} (s(p) + r(p)P_p(\text{reject}))$$

- The average cost for a productive system is

$$C_a = E_Q[C(p)|p \leq p_a]$$

# Checking a Batch (1) The simple sequential test

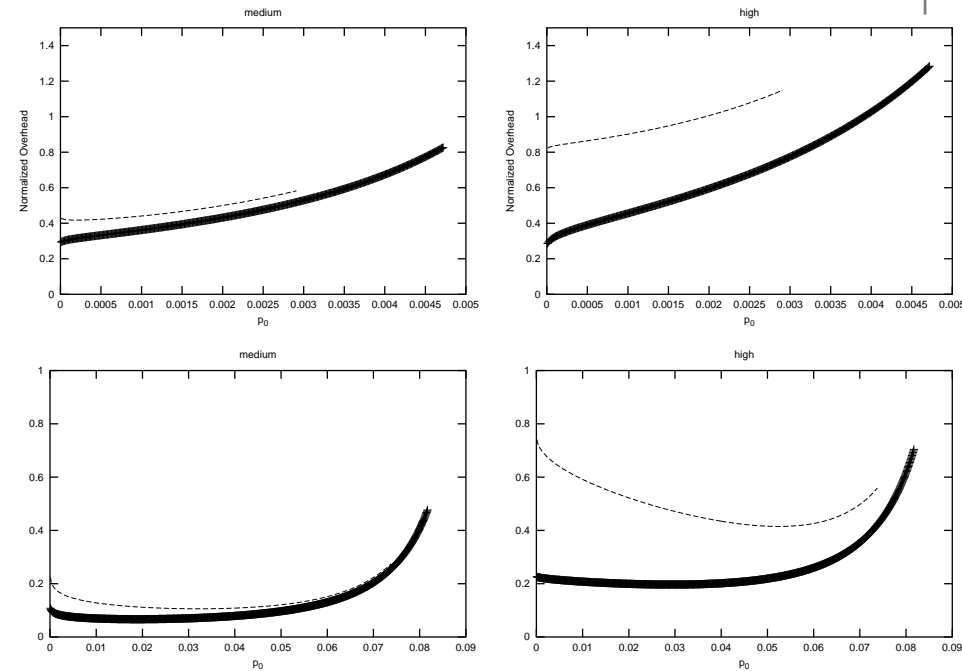
- Acceptable performance for the Normal case
  - The cost is dominated by the number of calls to the oracle
- Vulnerable to denial of service
  - With a uniform distribution of  $p$ , the decision of rejection should be reached earlier



Cost breakdown.  $\alpha = \beta = 0.05$ ,  $B = 1000$ ,  
 $p_a = 0.1$  (lower),  $p_a = 0.01$  (upper),  
 $\lambda = 0.01, 0.1, 1$

# The two-phases test

- Algorithm
  - First step : sense the system - time-sequential test
  - Second step : Test the whole batch
- *Normal and Massive* : Same cost
- *Denial of service* : Much more robust



$$\alpha = \beta = 0.05, B = 1000,$$
$$p_\alpha = 0.1 \text{ (lower), } p_\alpha = 0.01 \text{ (upper),}$$
$$\lambda = 0.1, 1$$