



# Activities on TCP

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# TCP behavior (summary)

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## □ State variables:

- CWND = Congestion Window (Congestion Control)
  - RCWND = Receiver Window (Flow Control)
  - SSTHRESH = Slow Start Threshold
  - MSS = Maximum Segment Size
  - RTO = Retransmission TimeOut
- } All expressed as multiples of MSS

## □ Initial values for all state variables (i.e., when the TCP connection is created):

- CWND=1
- RCWND = it depends (it's the dimension of the receiver buffer. In our exercises it will be explicitly given. Otherwise, we will assume it is *infinite*)
- SSTHRESH = infinite (sometimes, in our exercises, I will specify a finite, given value)
- MSS = it is determined in the 3-way handshake phase (MSS option). In our exercises, its value will always be explicitly given.
- RTO = in our exercises, its value will always be explicitly given

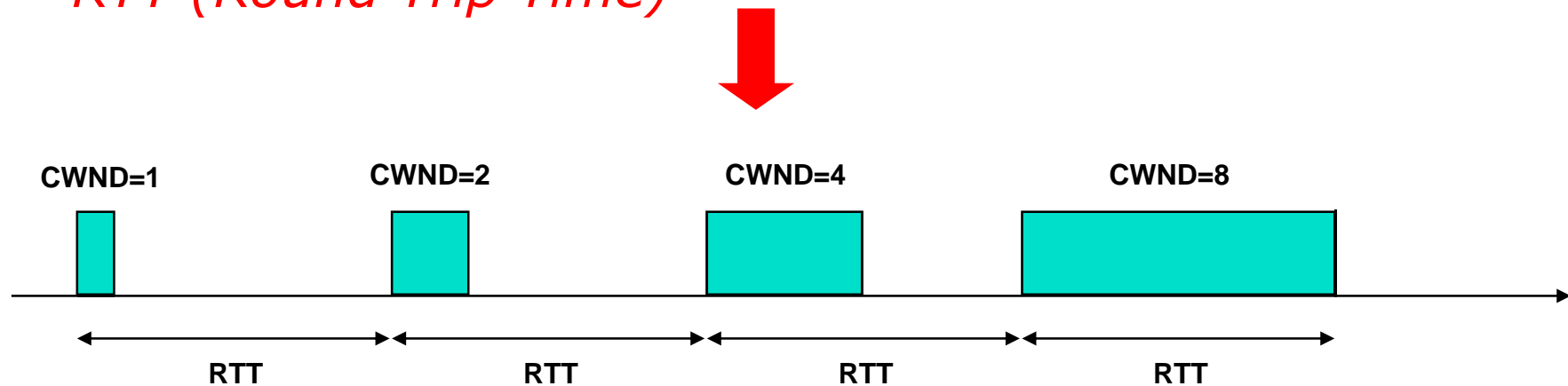


- For every sent packet, the sender starts a timer
- If the sender does *not* receive an ACK for a segment BEFORE the timer = RTO, the segment is considered lost and is retransmitted

# TCP behavior (Slow Start)

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- At the beginning of the TCP connection:  
CWND < SSTHRESH (in fact,  $1 < \text{infinite}$  !!!)
- Since  $\text{CWND} < \text{SSTHRESH}$ , the TCP connection is in *Slow Start*
- *In Slow Start:*
  - *CWND is incremented by 1 for each received ACK (exponential increase)*
- *In practice: in Slow Start, the CWND doubles in each RTT (Round Trip Time)*



## TCP Congestion Event (= packet loss)

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- When a packet is lost (the corresponding RTO expires), TCP performs the following operations:
  - TCP first updates the Ssthresh value according to the following equation

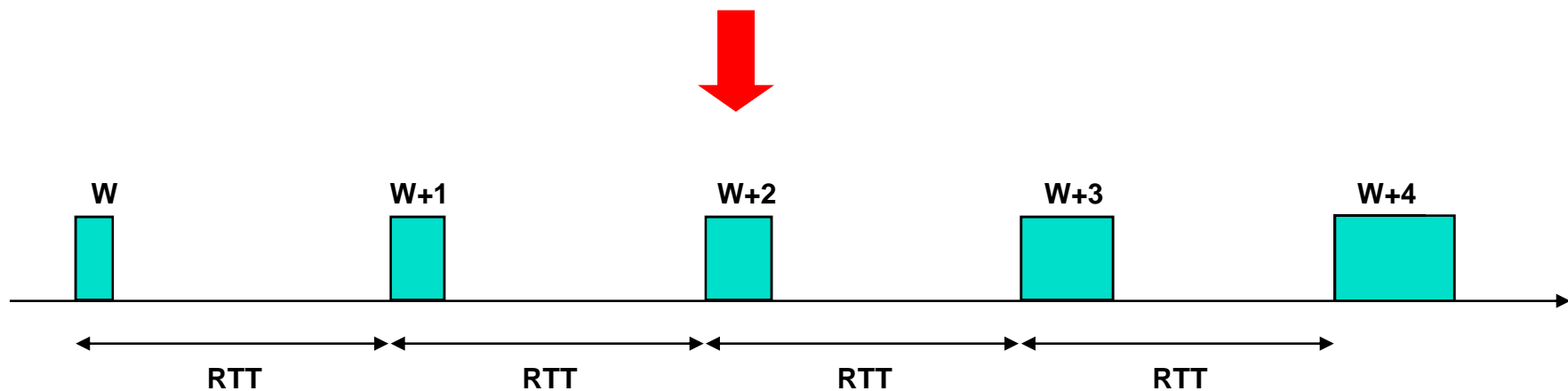
$$Ssthresh = \max\left(2, \frac{cwnd}{2}\right)$$

- And then sets  $cwnd = 1$
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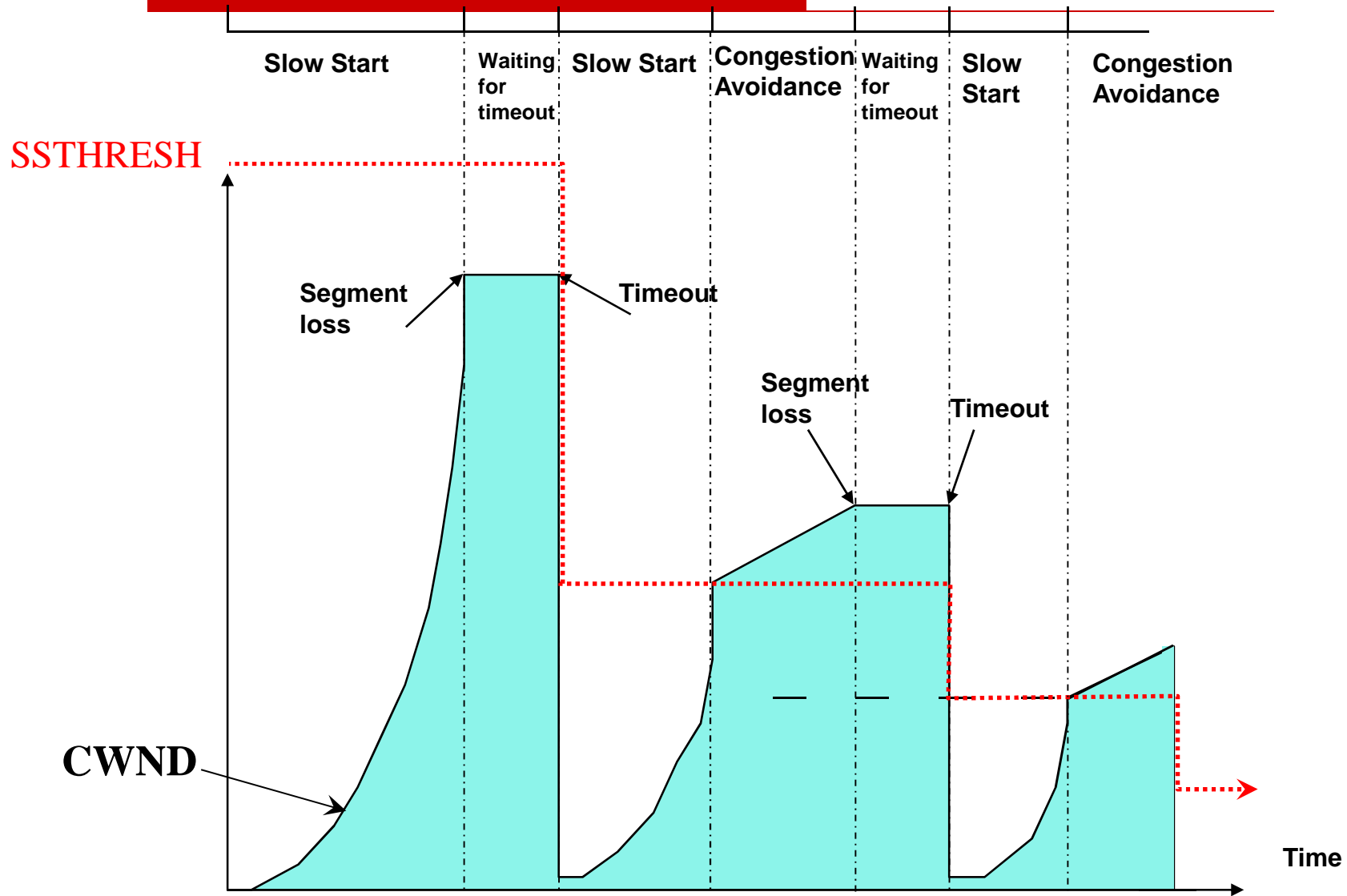
# TCP behavior (Congestion Avoidance)

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- If  $CWND \geq Ssthresh$ , TCP is in the so-called *Congestion Avoidance* phase
- In *Congestion Avoidance*:
  - $CWND$  is incremented by  $1/CWND$  for each received ACK (linear increase)
- In other words, the  $CWND$  increases by 1 in each RTT (linear increase)

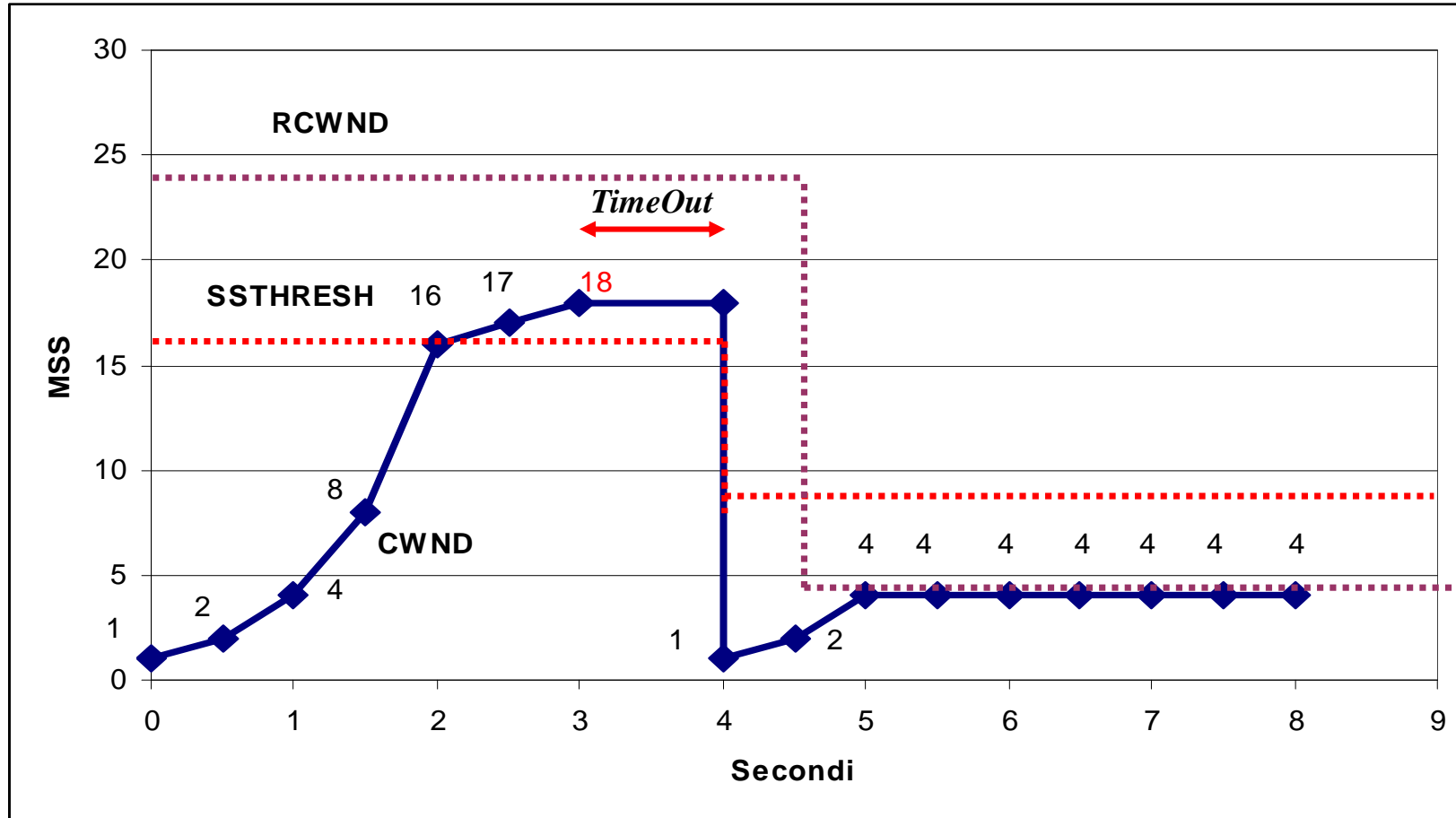


# TCP Connection Lifetime: example 1 (here RCWND = Infinite)



# TCP Connection Lifetime: example 2

(here both **SSTHRESH** and **RCWND** are **GIVEN**)

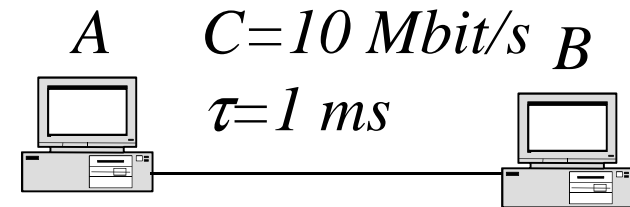


# Activity 1 (“Warm Up”)

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A single-hop TCP connection, running since long time (*steady state*) on a single link of capacity  $C$  and propagation delay  $\tau$ , is characterized by the following parameters:

1. Link capacity  $C = 10$  [Mbit/s]
2. Propagation delay  $\tau = 1$  [ms]
3.  $MSS = 100$  [byte]
4.  $RCWND = 4 MSS$  and  $RCWND \ll CWND$   
(this means that the connection is “dominated” by flow control, that is, by the  $RCWND$  value)
5. Let us assume the TCP *ACK* segments have negligible length (i.e., length = 0)

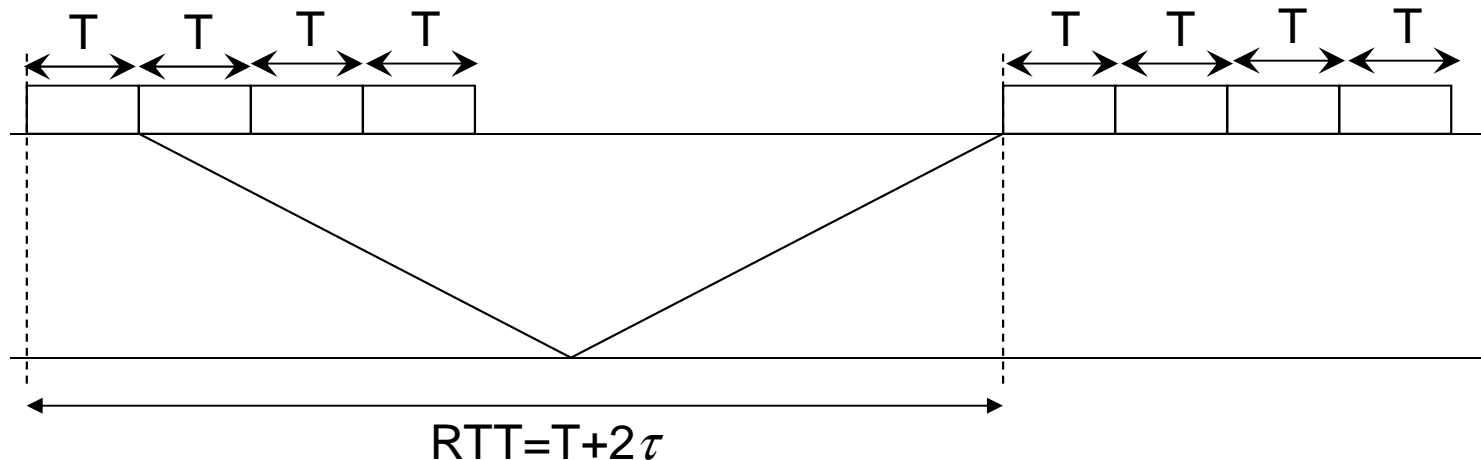


- D1. What is the average transmission rate of the TCP connection?
- D2. Answer to the same question assuming  $MSS = 1000$  byte.
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# Solution 1 (“Warm Up”)

- $T = 100 \times 8 \text{ [bits]} / 10 \text{ [Mbit/s]} = 0.08 \text{ ms}$ ,
- $RTT = T + 2\tau = 2.08 \text{ ms}$
- Hence  $4T < RTT$  (see figure below). Consequently, the transmission is *never* continuous, in this case.

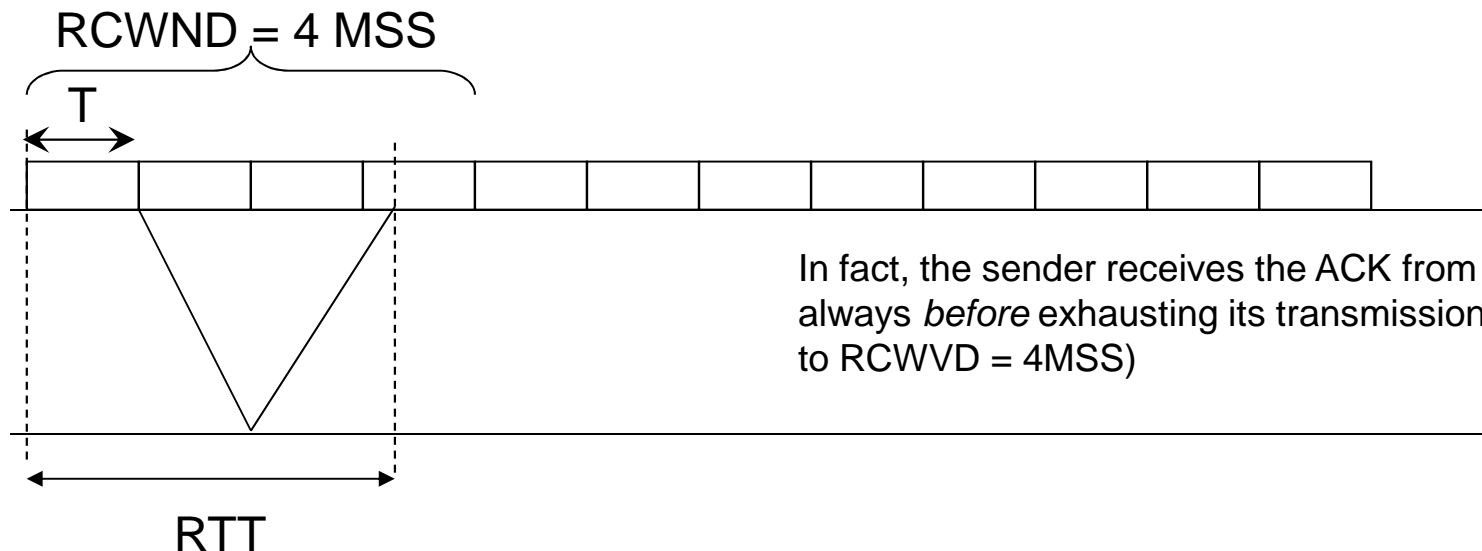


- Thus, the connection delivers 4 MSS for each RTT. Therefore, the average transmission rate,  $R$ , is:

$$R = \frac{4 \cdot (100 \cdot 8) \text{ bit}}{RTT} = \frac{3200 \text{ bit}}{2.08 \text{ ms}} \approx 1.54 \text{ Mbit/s}$$

# Solution 1 (“Warm Up”)

- In the second case
  - $T = 1000 \times 8 \text{ [bits]} / 10 \text{ [Mbit/s]} = 0.8 \text{ ms}$ ,
  - $RTT = T + 2\tau = 2.8 \text{ ms}$
  - Hence,  $4T = 3.2 \text{ ms}$ . Therefore,  $4T > RTT$ , and consequently the transmission is continuous and the rate is  $R = C = 10 \text{ Mbit/s}$ .



In fact, the sender receives the ACK from the receiver always *before* exhausting its transmission credit (equal to RCWVD = 4MSS)

# Activity 2

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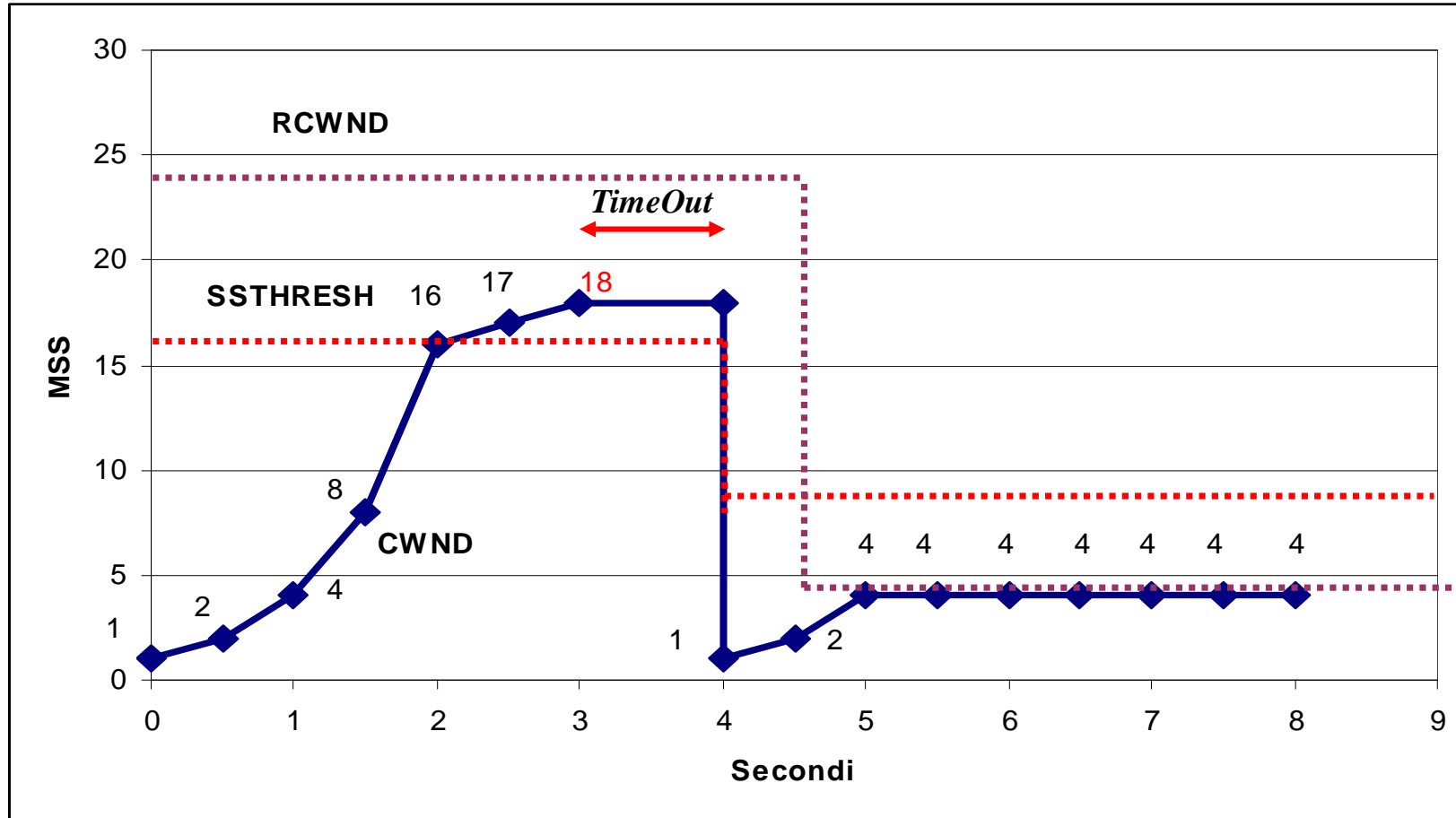
- A TCP connection is used to transfer a 39.5 [kbyte] file.
    - MSS=500 [byte]
    - RTT = 500 [ms]
    - Retransmission TimeOut RTO = 2\*RTT.
  - Assume the following parameter setting:
    - RCWND = 12 [kbyte]
    - Ssthresh = 8 [kbyte]
    - CWND = 500 [byte]
  - And further,
    - All the segments transmitted at time 3 [s] are lost
    - At time 4,5 [s] the receiver signals to the sender that RCWND = 2 [kbyte]
  - 1. Plot the time behavior of the following state variables:
    - CWND
    - Ssthresh
    - RCWND
  - 2. Find out the total delivery time for the aforementioned file.
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## **Solution 2**

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- ❑ File dimension (in MSS) =  $39,5 \text{ [kbyte]} / 500 \text{ [byte]} = 79 \text{ MSS}$
  - ❑ Total delivery time = time to transfer 79 MSS
  
  - ❑ RCWND =  $12 \text{ [kbyte]} / 500 \text{ [byte]} = 24 \text{ MSS}$
  - ❑ SSTHRESH =  $8 \text{ [kbyte]} / 500 \text{ [byte]} = 16 \text{ MSS}$
  - ❑ Time Out = 1 [s]
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# Solution 2

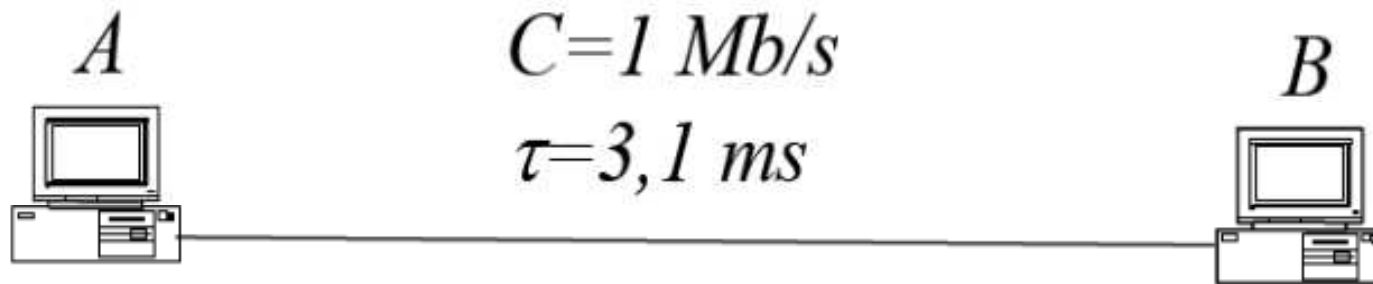


□ Total delivery time,  $T=8.5s$

# Activity 3

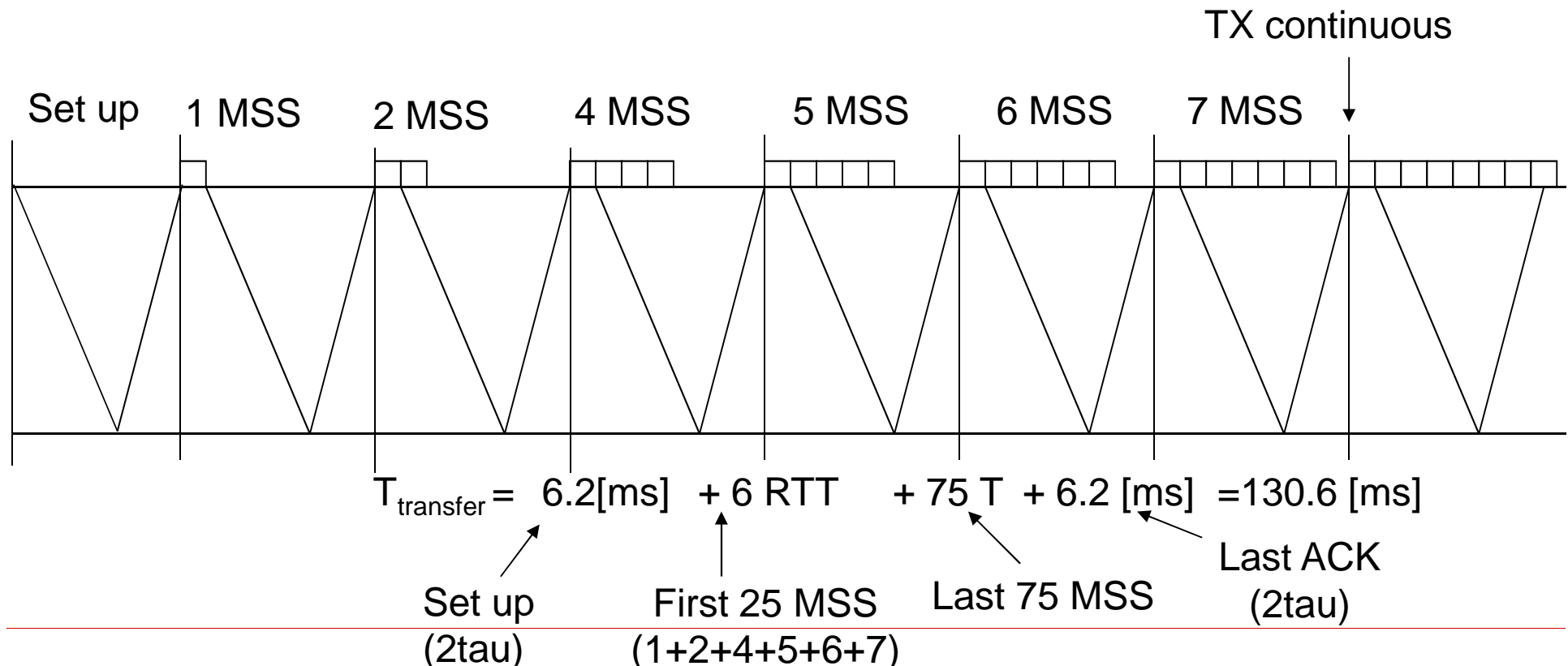
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- A must transfer 100 MSS segments to B through a TCP connection. Find out the total data delivery time, assuming:
  - MSS=1000 [bit]
  - Negligible headers
  - Connection is initiated by A, connection opening segment of negligible length
  - ACK segment length negligible
  - SSTHRESH = 5 MSS



# Solution 3

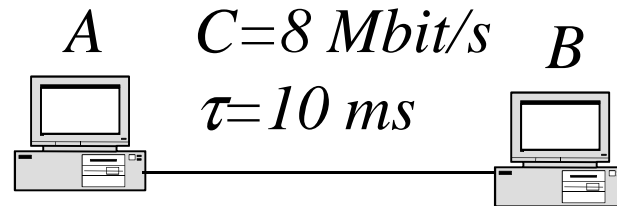
- $T = 1000 \text{ [bit]} / 1 \text{ [Mbit/s]} = 1 \text{ [ms]}$
- $RTT = T + 2\tau = T + 2 * 3.1 \text{ [ms]} = 7.2 \text{ [ms]}$
- Transmission is continuous when  $WT > RTT$ , hence until  $W=8$



# Activity 4, case A

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- Let us consider the following network



- **A establishes a TCP connection with B, and transfers 18 kbytes towards B**
    - Find out the total delivery time with the following assumptions:
      - MSS=1000 byte
      - Negligible header lengths
      - The connection is opened by A, and the messages exchanged during the connection setup have negligible length
      - Negligible ACK lengths
      - Ssthresh = 4 MSS
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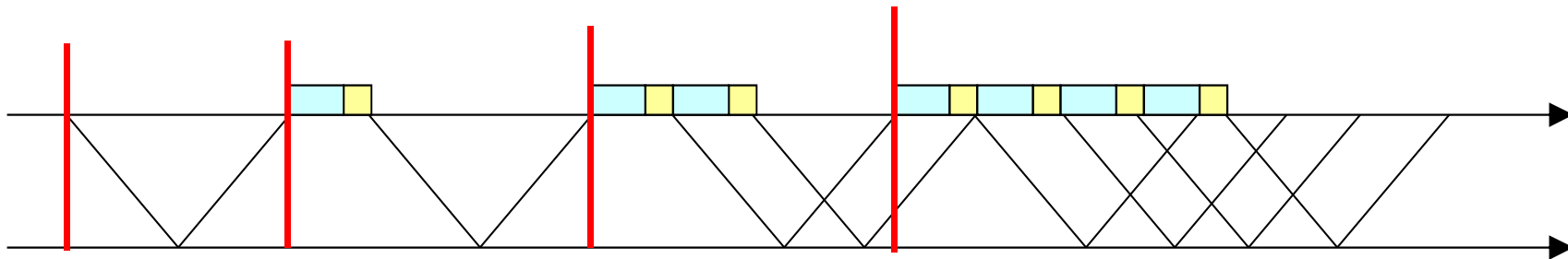


# Solution 4, case A

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$$T = 1 \text{ ms}$$

$$n = 18 \text{ segments}$$



$$1 + 2 + 4 + 5 + 6 = 18$$

$$T_{tot} = 2\tau + (T + 2\tau) + (T + 2\tau) + (T + 2\tau) + (T + 2\tau) + (T + 2\tau) + (6-1)T$$

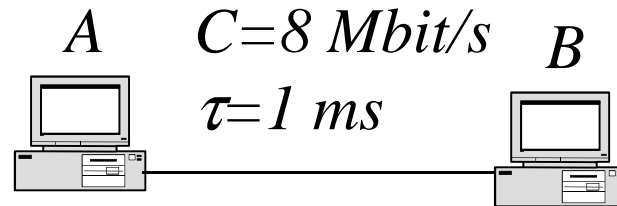
$$T_{tot} = 2\tau + 5(T + 2\tau) + (6-1)T = 12\tau + 10T = 130 \text{ ms}$$

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# Activity 4, case B

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- Let us consider the following network



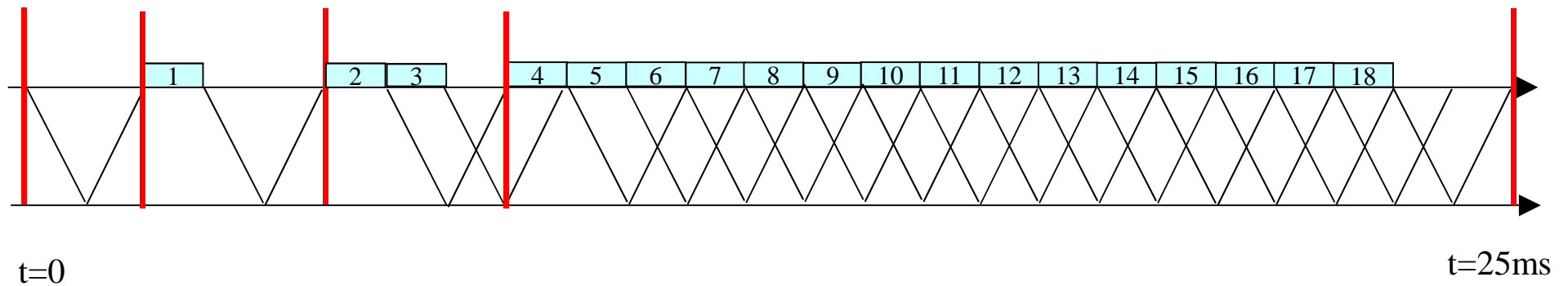
- **A establishes a TCP connection with B, and transfers 18 kbytes towards B**
    - Find out the total delivery time with the following assumptions:
      - MSS=1000 byte
      - Negligible header lengths
      - The connection is opened by A, and the messages exchanged during the connection setup have negligible length
      - Negligible ACK lengths
      - Ssthresh = 4 MSS
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# Solution 4, case B

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$$T = 1 \text{ ms}$$

$$n = 18 \text{ segments}$$



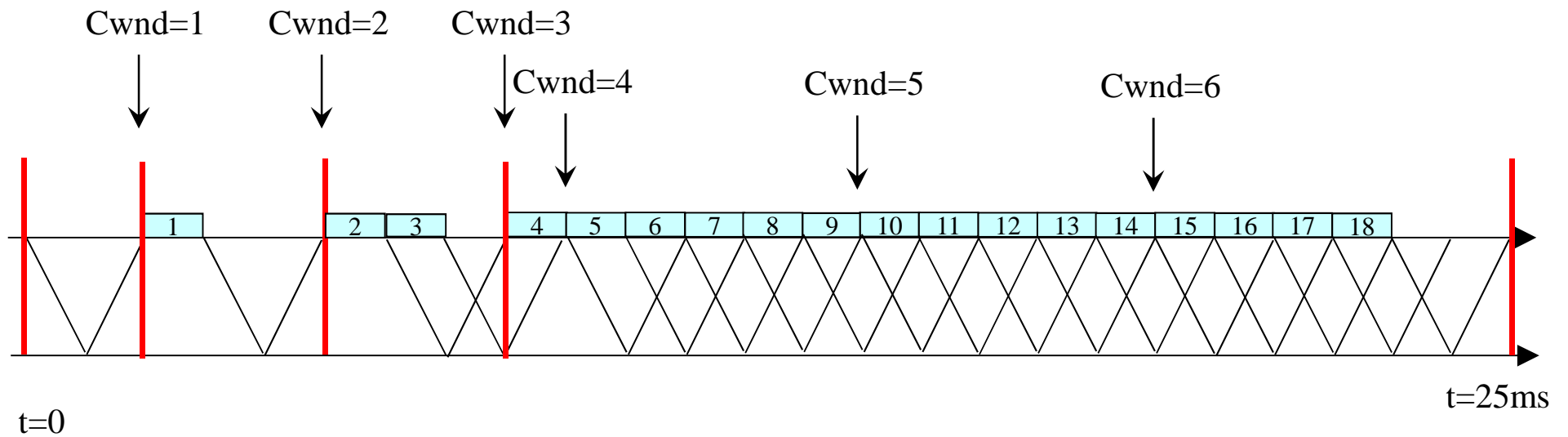
$$T_{tot} = 2\tau + (T + 2\tau) + (T + 2\tau) + (15T + 2\tau)$$

$$T_{tot} = 8\tau + 17T = 8 + 17 \text{ ms} = 25 \text{ ms}$$

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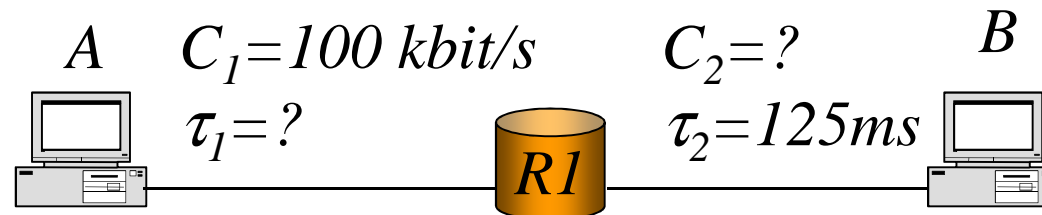
# Solution 4, case B

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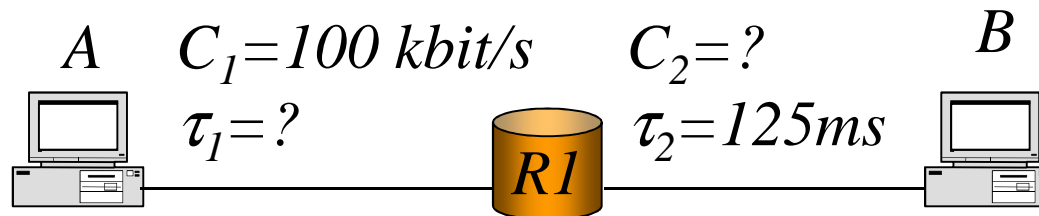
# Exercise 5 (“Network Tomography”)

- Given the multi-hop link in the figure:

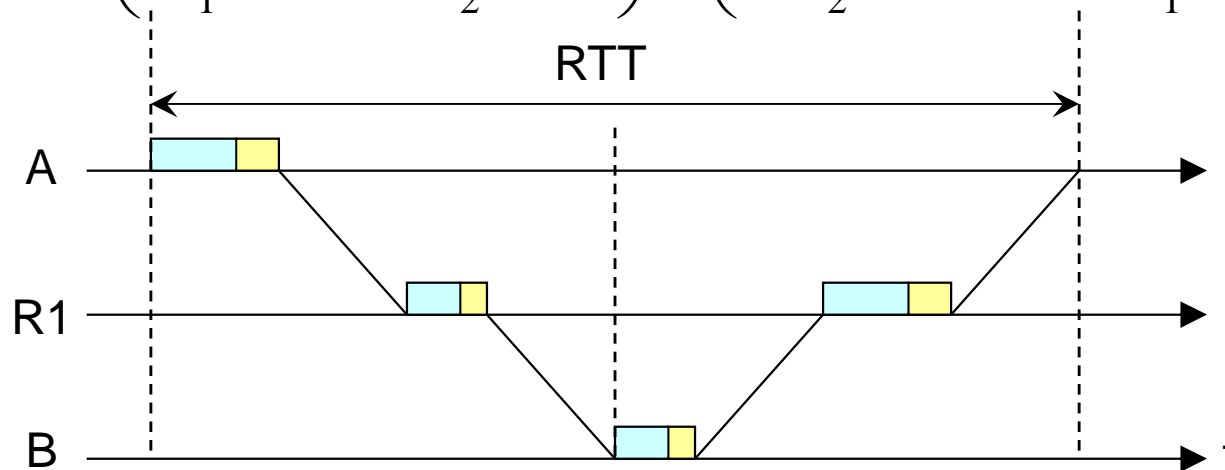


- A wants to estimate the propagation delay ( $\tau_1$ ) on link 1 and the Capacity ( $C_2$ ) on link 2.
- To this end, A sends 2 packets (that is, two *echo requests*) to B (with length  $m_1 = 500$  [byte],  $m_2 = 1000$  [byte], respectively), and B answers (immediately after he receives the packet from A) each time with packets of fixed length (*echo replies*). The length of each reply is  $m_{ACK} = 125$  [byte].
- A measures the following RTTs for the two packets:
  - $RTT_1 = 420$  [ms]
  - $RTT_2 = 540$  [ms]
- Find out  $\tau_1$  and  $C_2$  as estimated by A

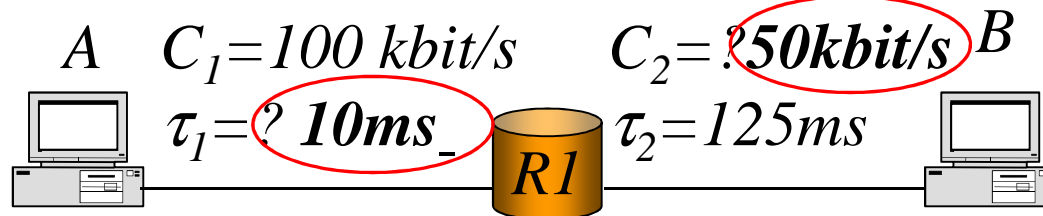
# Solution 5



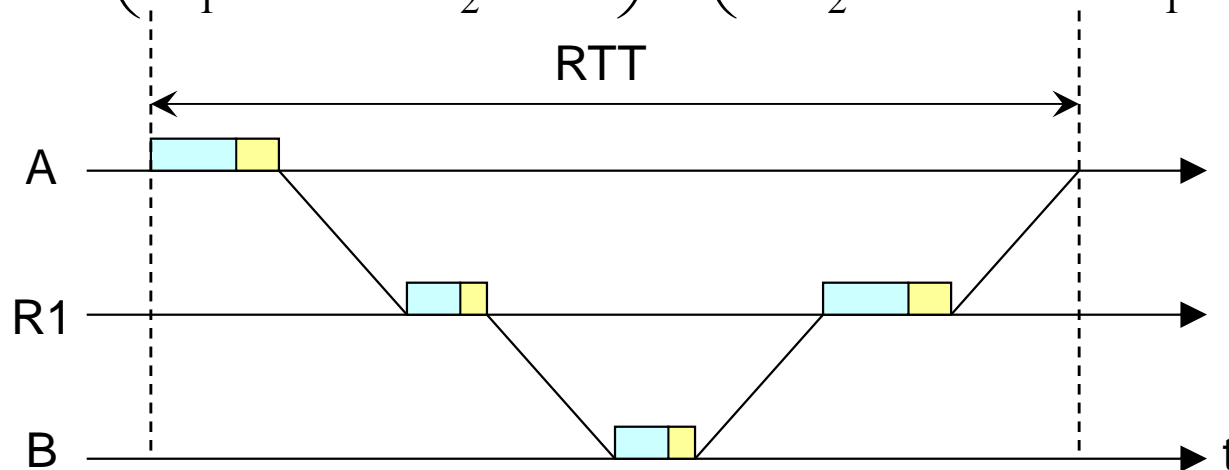
$$\left\{ \begin{aligned}
 RTT_1 &= \left( \frac{m_1}{C_1} + \tau_1 + \frac{m_1}{C_2} + \tau_2 \right) + \left( \frac{m_{ACK}}{C_2} + \tau_2 + \frac{m_{ACK}}{C_1} + \tau_1 \right) \\
 RTT_2 &= \left( \frac{m_2}{C_1} + \tau_1 + \frac{m_2}{C_2} + \tau_2 \right) + \left( \frac{m_{ACK}}{C_2} + \tau_2 + \frac{m_{ACK}}{C_1} + \tau_1 \right)
 \end{aligned} \right.$$



# Solution 5



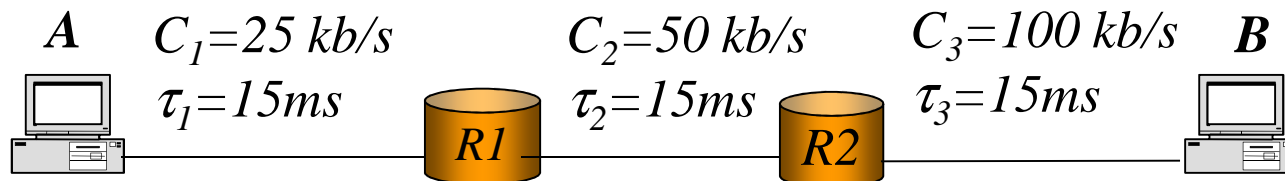
$$\left\{ \begin{aligned}
 RTT_1 &= \left( \frac{m_1}{C_1} + \tau_1 + \frac{m_1}{C_2} + \tau_2 \right) + \left( \frac{m_{ACK}}{C_2} + \tau_2 + \frac{m_{ACK}}{C_1} + \tau_1 \right) \\
 RTT_2 &= \left( \frac{m_2}{C_1} + \tau_1 + \frac{m_2}{C_2} + \tau_2 \right) + \left( \frac{m_{ACK}}{C_2} + \tau_2 + \frac{m_{ACK}}{C_1} + \tau_1 \right)
 \end{aligned} \right.$$



# Activity 6

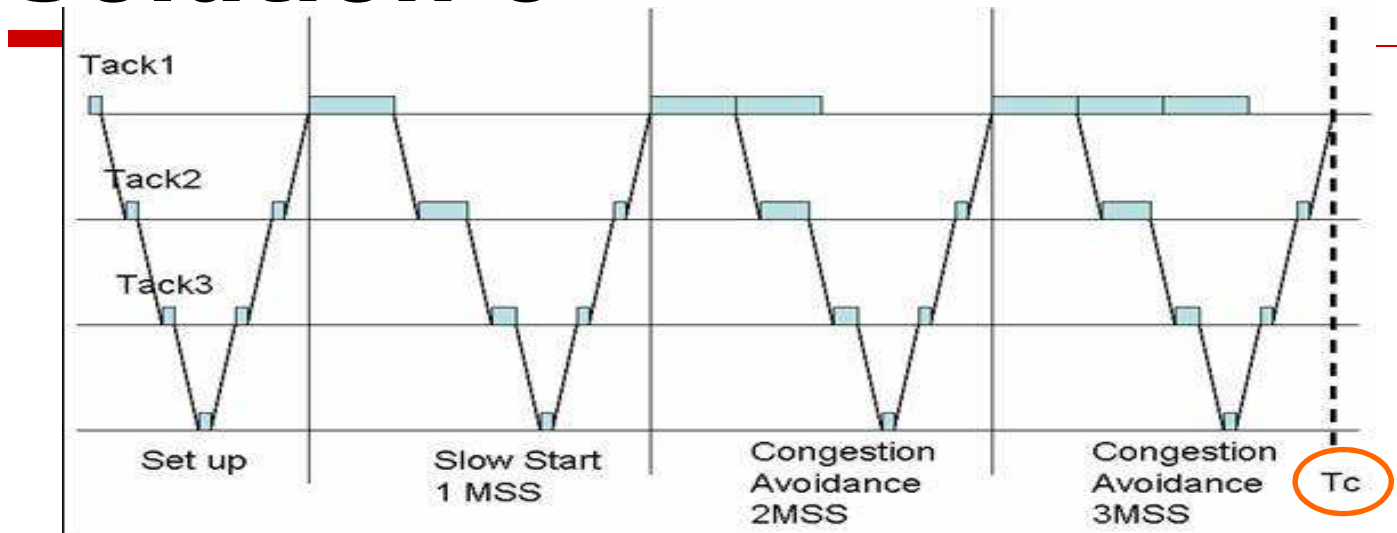
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1. At time  $t=0$ , A initiates a TCP connection towards B. Find out the time  $T_C$  at which the transmission on link 1 becomes continuous, assuming:
  - Negligible header lengths
  - Bidirectional links
  - RCWND = 4000 [byte] and SSTHRESH = 400 [byte]
  - MSS = 200 [byte]
  - ACK length = opening connection segments length = 20 [byte]
2. Find out the total delivery time for a file of 2 [kbyte] (including connection set-up time)
  - (1 byte = 8 bit, 1 kbyte = 1000 byte = 8000 bit)





# Solution 6



- Some numbers:
  - $T_1 = 200 \times 8 \text{ [bit]} / 25 \text{ [kbit/s]} = 64 \text{ ms}$ ,  $T_2 = \frac{1}{2} T_1 = 32 \text{ ms}$ ,  
 $T_3 = \frac{1}{2} T_2 = 16 \text{ ms}$
  - $T_{ack1} = 6.4 \text{ ms}$ ,  $T_{ack2} = 3.2 \text{ ms}$ ,  $T_{ack3} = 1.6 \text{ ms}$
  - $RTT = T_1 + T_2 + T_3 + 2(\tau_1 + \tau_2 + \tau_3) + T_{ack1} + T_{ack2} + T_{ack3} = 213.2 \text{ ms}$
  - $T_{setup} = 2(T_{ack1} + T_{ack2} + T_{ack3}) + 2(\tau_1 + \tau_2 + \tau_3) = 112.4 \text{ ms}$
- Link 1 is the bottleneck, transmission is continuous when:
  - $WT_1 > RTT$
- thus
  - $W > RTT / T_1 = 3,3$
- Consequently, the time for the transmission to become continuous is
  - $T_c = T_{setup} + 3 RTT = 112.4 \text{ [ms]} + 649.6 \text{ [ms]} = 752 \text{ [ms]}$

# Solution 6

- 2 [kbyte] file is equivalent to 10 MSS.
- Total delivery time is given by:
  - $T_{\text{tot}} = T_{\text{setup}} + 4 \text{ RTT} + 3 T_1 = 1.15 \text{ [s]}$

