

L3 Apprentissage

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LRI – LSV

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Overview

The AI roots of ML, foll'd

Introduction to Supervised Machine Learning

Decision trees

Empirical validation

- Performance indicators

- Estimating an indicator

La promesse (1960)

Within 10 years, a computer will

- ▶ be the world's chess champion
- ▶ prove an important theorem in maths
- ▶ compose good music
- ▶ set up the language for theoretical psychology

L'IA a beaucoup promis

The world's chess champion ?



Discussion

Entre intelligence et force brute.

L'IA a beaucoup promis, 2

Prouver un théorème ?



The robot scientist

- ▶ Faits $\rightarrow$ Hypothèses
 - ▶ Hypothèses $\rightarrow$ Expériences
 - ▶ Expériences $\rightarrow$ Faits
-
- ▶ King R. D., Whelan, K. E., Jones, F. M., Reiser, P. G. K., Bryant, C. H., Muggleton, S., Kell, D. B. and Oliver, S. G. (2004) Functional genomic hypothesis generation and experimentation by a robot scientist. *Nature* 427 (6971) p247-252
 - ▶ King R.D., Rowland J., Oliver S.G, Young M., Aubrey W., Byrne E., Liakata M., Markham M., Pir P., Soldatova L., Sparkes A., Whelan K.E., Clare A. (2009). The Automation of Science. *Science* 324 (5923): 85-89, 3rd April 2009

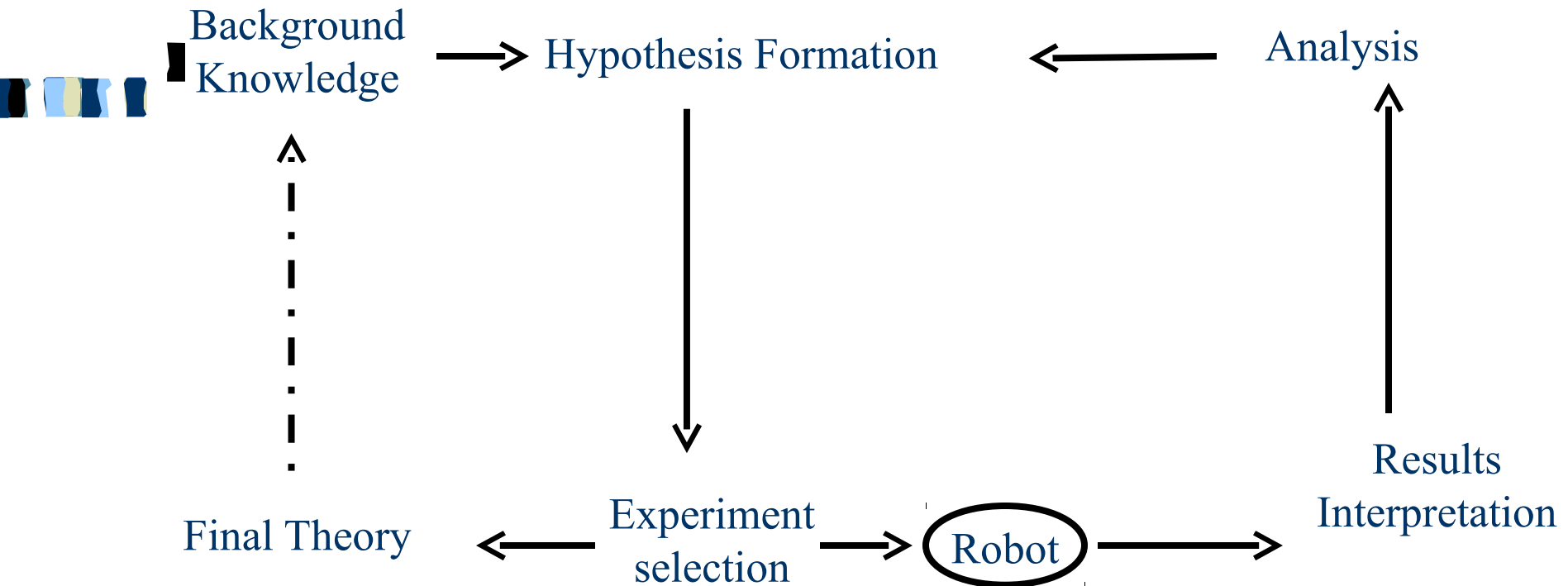
Automating Biology Using Robot Scientists

Ross D. King,
University of Manchester, ross.king@manchester.ac.uk



The Concept of a Robot Scientist

Computer systems capable of originating their own experiments, physically executing them, interpreting the results, and then repeating the cycle.



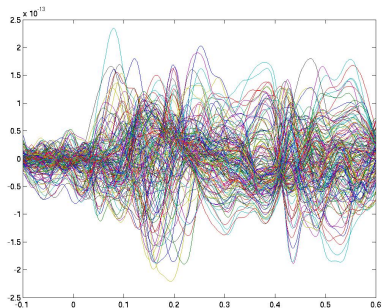
L'IA a beaucoup promis, 3

Composer de la bonne musique ?

Musac

L'IA a beaucoup promis, 4

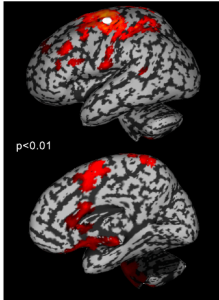
Set up the language for theoretical psychology ?



Neuro-imagerie — Interfaces Cerveau-Machine

L'IA a beaucoup promis, 4

Set up the language for theoretical psychology ?



Test d'hypothèses multiples

http://videolectures.net/msht07_baillet_mht/

Lessons from 50 years

- ▶ We need descriptive knowledge: perceptual primitives, patterns, constraints, rules,
- ▶ We need control knowledge: policy, adaptation
- ▶ Knowledge can hardly be given: must be acquired
- ▶ We need interaction knowledge: retrieving new information, feedback

Meta-knowledge

J. Pitrat, 2009

- ▶ Each goal, a new learning algorithm ?
- ▶ Problem reduction ? John Langford, <http://hunch.net/>

Artificial Intelligence

Search space

- ▶ Representation
- ▶ Patterns, Rules, Constraints (knowledge)
- ▶ Navigation policy

ML

(Un) Supervised L.

(Un) Supervised L., Data Mining

Reinforcement L.

Navigation

- ▶ Inference

Optimisation

Validation, control, feedback

- ▶ Criteria

Statistics

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Types of Machine Learning problems

WORLD – DATA – USER

Observations

+ **Target**

+ Rewards

**Understand
Code**

**Predict
Classification/Regression**

**Decide
Policy**

**Unsupervised
LEARNING**

**Supervised
LEARNING**

**Reinforcement
LEARNING**

Data

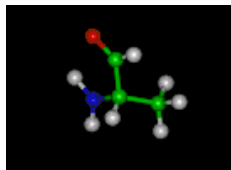
Example

- ▶ row : example/ case
- ▶ column : feature/ variable/ attribute
- ▶ attribute : class/ label

age	employment	education	educ	marital	...	job	relation	race	gender	hours	country	wealth
39	State_gov	Bachelors	13	Never_mar	...	Adm_clerk	Not_in_fan	White	Male	40	United_States	poor
51	Self_employed	Bachelors	13	Married	...	Exec_manager	Husband	White	Male	13	United_States	poor
39	Private	HS_grad	9	Divorced	...	Handlers_cleaners	Not_in_fan	White	Male	40	United_States	poor
54	Private	11th	7	Married	...	Handlers_cleaners	Husband	Black	Male	40	United_States	poor
28	Private	Bachelors	13	Married	...	Prof_spec	Wife	Black	Female	40	Cuba	poor
38	Private	Masters	14	Married	...	Exec_manager	Wife	White	Female	40	United_States	poor
50	Private	9th	5	Married_spouse	...	Other_serv	Not_in_fan	Black	Female	16	Jamaica	poor
52	Self_employed	HS_grad	9	Married	...	Exec_manager	Husband	White	Male	45	United_States	rich
31	Private	Masters	14	Never_mar	...	Prof_spec	Not_in_fan	White	Female	50	United_States	rich
42	Private	Bachelors	13	Married	...	Exec_manager	Husband	White	Male	40	United_States	rich
37	Private	Some_college	10	Married	...	Exec_manager	Husband	Black	Male	80	United_States	rich
30	State_gov	Bachelors	13	Married	...	Prof_spec	Husband	Asian	Male	40	India	rich
24	Private	Bachelors	13	Never_mar	...	Adm_clerk	Own_child	White	Female	30	United_States	poor
33	Private	Assoc_degree	12	Never_mar	...	Sales	Not_in_fan	Black	Male	50	United_States	poor
41	Private	Assoc_voc	11	Married	...	Craft_repair	Husband	Asian	Male	40	MissingV	rich
34	Private	7th_8th	4	Married	...	Transportation	Husband	Amer_Indi	Male	45	Mexico	poor
26	Self_employed	HS_grad	9	Never_mar	...	Farming_fishery	Own_child	White	Male	35	United_States	poor
33	Private	HS_grad	9	Never_mar	...	Machine_cleaner	Unmarried	White	Male	40	United_States	poor
38	Private	11th	7	Married	...	Sales	Husband	White	Male	50	United_States	poor
44	Self_employed	Masters	14	Divorced	...	Exec_manager	Unmarried	White	Female	45	United_States	rich
41	Private	Doctorate	16	Married	...	Prof_spec	Husband	White	Male	60	United_States	rich
:	:	:	:	:	:	:	:	:	:	:	:	:

Instance space $\mathcal{X}$

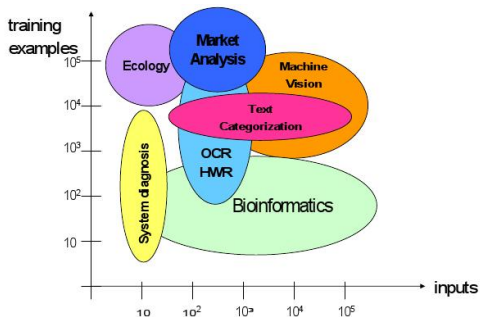
- ▶ Propositional :
 $\mathcal{X} \equiv \mathbb{R}^d$
- ▶ Structured :
sequential,
spatio-temporal,
relational.



aminoacid

Data / Applications

- ▶ Propositional data 80% des applis.
- ▶ Spatio-temporal data alarms, mines, accidents
- ▶ Relational data chemistry, biology
- ▶ Semi-structured data text, Web
- ▶ Multi-media images, music, movies,...



Difficulty factors

Quality of data / of representation

- Noise; missing data
 - + Relevant attributes
 - Structured data: spatio-temporal, relational, text, videos,..
- Feature extraction**

Data distribution

- + Independants, identically distributed examples
- Other: robotics; data streams; heterogeneous data

Prior knowledge

- + Goals, interestingness criteria
- + Constraints on target hypotheses

Difficulty factors, 2

Learning criterion

- + Convex optimization problem
- ↘ Complexity : n , $n \log n$, n^2
- Combinatorial optimization

Scalability

H. Simon, 1958:

In complex real-world situations, optimization becomes approximate optimization since the description of the real-world is radically simplified until reduced to a degree of complication that the decision maker can handle.

Satisficing seeks simplification in a somewhat different direction, retaining more of the detail of the real-world situation, but settling for a satisfactory, rather than approximate-best, decision.

Learning criteria, 2

The user's criteria

- ▶ Relevance, causality,
- ▶ INTELLIGIBILITY
- ▶ Simplicity
- ▶ Stability
- ▶ Interactive processing, visualisation
- ▶ ... Preference learning

Difficulty factors, 3

Crossing the chasm

- ▶ No *killer algorithm*
- ▶ Little expertise about algorithm selection

How to assess an algorithm

- ▶ Consistency

When number n of examples goes to infinity
and target concept h^* is in $\mathcal{H}$
 h^* is found:

$$\lim_{n \rightarrow \infty} h_n = h^*$$

- ▶ Speed of convergence

$$\|h^* - h_n\| = \mathcal{O}(1/n), \mathcal{O}(1/\sqrt{n}), \mathcal{O}(1/\ln n)$$

Context

Disciplines et critères

- ▶ Data bases, Data Mining

Scalability

- ▶ Statistics, data analysis

Predefined models

- ▶ Machine learning

Prior knowledge; complex data/hypotheses

- ▶ Optimisation

well / ill posed problems

- ▶ Computer Human Interaction

No final solution: a process

- ▶ High performance computing

Distributed processing; safety

Supervised Learning, notations

Context

World $\rightarrow$ Instance $\mathbf{x}_i \rightarrow$ Oracle
 $\downarrow$
 y_i



INPUT

$\sim P(\mathbf{x}, y)$

$$\mathcal{E} = \{(\mathbf{x}_i, y_i), \mathbf{x}_i \in \mathcal{X}, y_i \in \mathcal{Y}, i = 1 \dots n\}$$

HYPOTHESIS SPACE

$$\mathcal{H} \quad h : \mathcal{X} \mapsto \mathcal{Y}$$

LOSS FUNCTION

$$\ell : \mathcal{Y} \times \mathcal{Y} \mapsto \mathbb{R}$$

OUTPUT

$$h^* = \arg \max \{ \text{score}(h), h \in \mathcal{H} \}$$

Classification and criteria

Supervised learning

- ▶ $\mathcal{Y} = \text{True/False}$ classification
- ▶ $\mathcal{Y} = \{1, \dots, k\}$ multi-class discrimination
- ▶ $\mathcal{Y} = \mathbb{R}$ regression

Generalization Error

$$Err(h) = E[\ell(y, h(\mathbf{x}))] = \int \ell(y, h(\mathbf{x})) dP(\mathbf{x}, y)$$

Empirical Error

$$Err_e(h) = \frac{1}{n} \sum_{i=1}^n \ell(y_i, h(\mathbf{x}_i))$$

Bound

structural risk

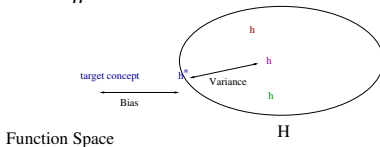
$$Err(h) < Err_e(h) + \mathcal{F}(n, d(\mathcal{H}))$$

$d(\mathcal{H}) =$ Vapnik Cervonenkis dimension of $\mathcal{H}$, see later

The Bias-Variance Trade-off

Bias Bias ($\mathcal{H}$): error of the best hypothesis h^* de $\mathcal{H}$

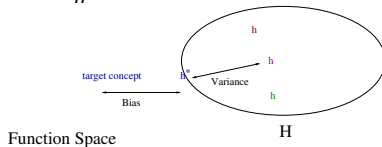
Variance Variance of h_n as a function of $\mathcal{E}$



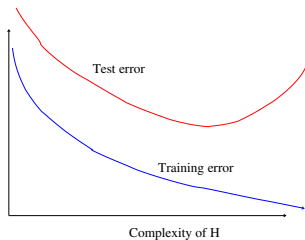
The Bias-Variance Trade-off

Bias Bias ($\mathcal{H}$): error of the best hypothesis h^* de $\mathcal{H}$

Variance Variance of h_n as a function of $\mathcal{E}$



Overfitting



Key notions

- ▶ The main issue regarding supervised learning is overfitting.
 - ▶ How to tackle overfitting:
 - ▶ Before learning: use a sound criterion
 - ▶ After learning: cross-validation
- regularization
Case studies

Summary

- ▶ Learning is a search problem
- ▶ What is the space ? What are the navigation operators ?

Hypothesis Spaces

Logical Spaces

$$\text{Concept} \leftarrow \bigvee \bigwedge \text{Literal, Condition}$$

- ▶ Conditions = [color = blue]; [age < 18]
- ▶ Condition $f : X \mapsto \{True, False\}$
- ▶ Find: disjunction of conjunctions of conditions
- ▶ Ex: (unions of) rectangles of the 2D-plane X .

Hypothesis Spaces

Numerical Spaces

Concept = $(h() > 0)$

- ▶ $h(x)$ = polynomial, neural network, ...
- ▶ $h : X \mapsto \mathbb{R}$
- ▶ Find: (structure and) parameters of h

Hypothesis Space $\mathcal{H}$

Logical Space

- ▶ h covers one example x iff $h(x) = \text{True}$.
- ▶ $\mathcal{H}$ is structured by a partial order relation

$$h \prec h' \text{ iff } \forall x, h(x) \rightarrow h'(x)$$

Numerical Space $\mathcal{H}$

- ▶ $h(x)$ is a real value (more or less far from 0)
- ▶ we can define $\ell(h(x), y)$
- ▶ $\mathcal{H}$ is structured by a partial order relation

$$h \prec h' \text{ iff } E[\ell(h(x), y)] < E[\ell(h'(x), y)]$$

Hypothesis Space $\mathcal{H}$ / Navigation

	$\mathcal{H}$	navigation operators
Version Space	Logical	spec / gen
Decision Trees	Logical	specialisation
Neural Networks	Numerical	gradient
Support Vector Machines	Numerical	quadratic opt.
Ensemble Methods	—	adaptation $\mathcal{E}$

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Decision trees

Empirical validation

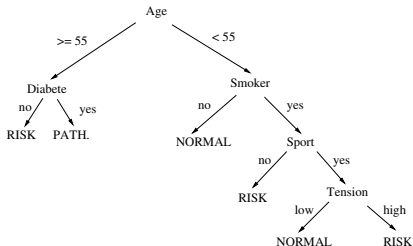
Performance indicators

Estimating an indicator

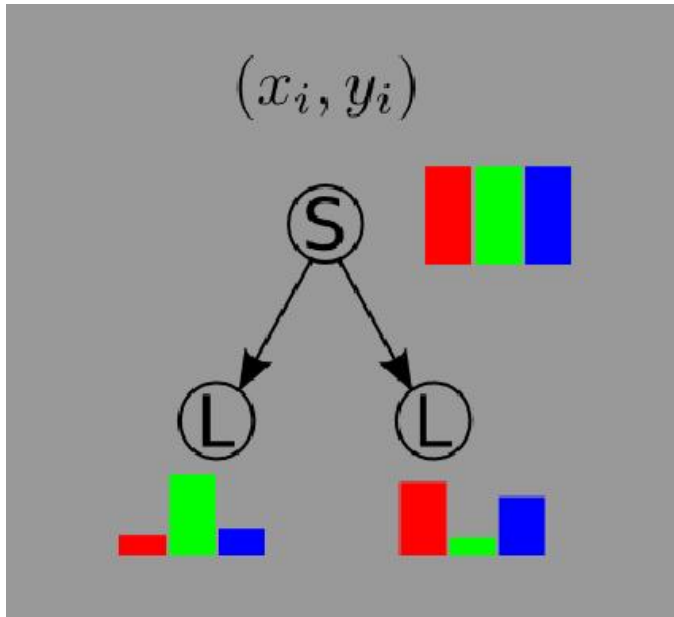
Decision Trees

C4.5 (Quinlan 86)

- ▶ Among the most widely used algorithms
- ▶ Easy
 - ▶ to understand
 - ▶ to implement
 - ▶ to use
 - ▶ and cheap in CPU time
- ▶ J48, Weka, SciKit



Decision Trees



Decision Trees (2)

Procedure DecisionTree($\mathcal{E}$)

1. Assume $\mathcal{E} = \{(x_i, y_i)_{i=1}^n, x_i \in \mathbb{R}^D, y_i \in \{0, 1\}\}$
 - If $\mathcal{E}$ single-class (i.e., $\forall i, j \in [1, n]; y_i = y_j$), return
 - If n too small (i.e., $< \text{threshold}$), return
 - Else, find the most informative attribute att
2. For all value val of att
 - Set $\mathcal{E}_{val} = \mathcal{E} \cap [att = val]$.
 - Call DecisionTree($\mathcal{E}_{val}$)

Criterion: information gain

$$\begin{aligned}p &= Pr(Class = 1 | att = val) \\ I([att = val]) &= -p \log p - (1 - p) \log (1 - p) \\ I(att) &= \sum_i Pr(att = val_i) \cdot I([att = val_i])\end{aligned}$$

Decision Trees (3)

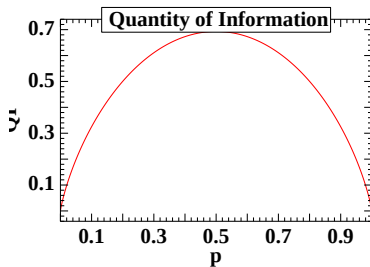
Contingency Table

wealth values:		poor	rich	
agegroup	10s	2507	3	
	20s	11262	743	
	30s	9468	3461	
	40s	6738	3986	
	50s	4110	2509	
	60s	2245	809	
	70s	668	147	
	80s	115	16	
	90s	42	13	

Computation

value	$p(\text{value})$	$p(\text{poor} \mid \text{value})$	QI (value)	$p(\text{value}) * \text{QI (value)}$
$[0,10[$	0.051	0.999	0.00924	0.000474
$[10,20[$	0.25	0.938	0.232	0.0570323
$[20,30[$	0.26	0.732	0.581	0.153715

Quantity of Information (QI)



Decision Trees (4)

Limitations

- ▶ XOR-like attributes
- ▶ Attributes with many values
- ▶ Numerical attributes
- ▶ Overfitting

Limitations

Numerical Attributes

- ▶ Order the values $val_1 < \dots < val_t$
- ▶ Compute $QI([att < val_i])$
- ▶ $QI(att) = \max_i QI([att < val_i])$

The XOR case

Bias the distribution of the examples

Complexity

Quantity of information of an attribute

$$n \ln n$$

Adding a node

$$D \times n \ln n$$

Tackling Overfitting

Penalize the selection of an already used variable

- ▶ Limits the tree depth.

Do not split subsets below a given minimal size

- ▶ Limits the tree depth.

Pruning

- ▶ Each leaf, one conjunction;
- ▶ Generalization by pruning literals;
- ▶ Greedy optimization, QI criterion.

Decision Trees, Summary

Still around after all these years

- ▶ Robust against noise and irrelevant attributes
- ▶ Good results, both in quality and complexity

Random Forests

Breiman 00

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Validation issues

1. What is the result ?
2. My results look good. Are they ?
3. Does my system outperform yours ?
4. How to set up my system ?

Validation: Three questions

Define a good indicator of quality

- ▶ Misclassification cost
- ▶ Area under the ROC curve

Computing an estimate thereof

- ▶ Validation set
- ▶ Cross-Validation
- ▶ Leave one out
- ▶ Bootstrap

Compare estimates: Tests and confidence levels

Which indicator, which estimate: depends.

Settings

- ▶ Large/few data

Data distribution

- ▶ Dependent/independent examples
- ▶ balanced/imbalanced classes

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Performance indicators

Binary class

- ▶ h^* the truth
- ▶ $\hat{h}$ the learned hypothesis

Confusion matrix

$\hat{h} / h^*$	1	0	
1	a	b	a+b
0	c	d	c+d
	a+c	b+d	a + b + c + d

Performance indicators, 2

$\hat{h} / h^*$	1	0	
1	a	b	a+b
0	c	d	c+d
	a+c	b+d	a + b + c + d

- ▶ Misclassification rate $\frac{b+c}{a+b+c+d}$
- ▶ Sensitivity (recall), True positive rate (TP) $\frac{a}{a+c}$
- ▶ Specificity, False negative rate (FN) $\frac{b}{b+d}$
- ▶ Precision $\frac{a}{a+b}$

Note: always compare to random guessing / baseline alg.

Performance indicators, 3

The Area under the ROC curve

- ▶ ROC: Receiver Operating Characteristics
- ▶ Origin: Signal Processing, Medicine

Principle

$h : X \mapsto \mathbb{R}$ $h(x)$ measures the risk of patient x

h leads to order the examples:

+ + + - + - + + + + - - - + - - - - - - - - - - - - - - - -

Performance indicators, 3

The Area under the ROC curve

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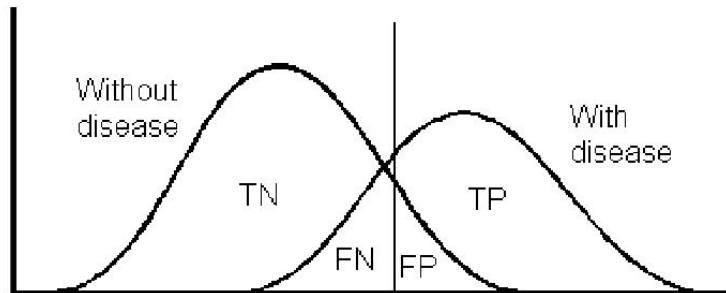
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Given a threshold θ , h yields a classifier: Yes iff $h(x) > \theta$.

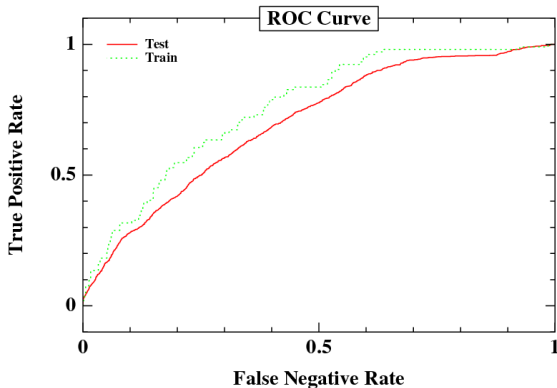
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Here, TP $(\theta) = .8$; FN $(\theta) = .1$

ROC



The ROC curve



Ideal classifier: (0 False negative, 1 True positive)

Diagonal (True Positive = False negative) $\equiv$ nothing learned.

ROC Curve, Properties

Properties

ROC depicts the trade-off True Positive / False Negative.

Standard: misclassification cost (Domingos, KDD 99)

$$\text{Error} = \# \text{ false positive} + c \times \# \text{ false negative}$$

In a multi-objective perspective, ROC = Pareto front.

Best solution: intersection of Pareto front with $\Delta(-c, -1)$

ROC Curve, Properties, foll'd

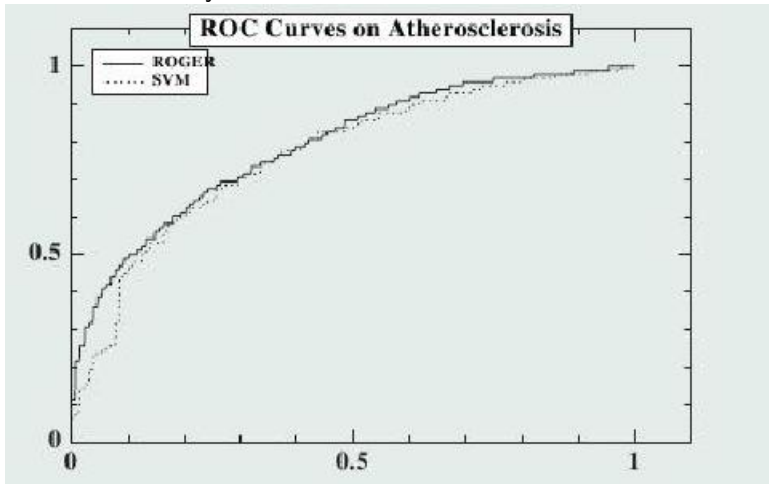
Used to compare learners

Bradley 97

multi-objective-like

insensitive to imbalanced distributions

shows sensitivity to error cost.



Area Under the ROC Curve

Often used to select a learner

Don't ever do this !

Hand, 09

Sometimes used as learning criterion

Mann Whitney

Wilcoxon

$$AUC = Pr(h(x) > h(x') | y > y')$$

WHY

Rosset, 04

- ▶ More stable $\mathcal{O}(n^2)$ vs $\mathcal{O}(n)$
- ▶ With a probabilistic interpretation

Clemençon et al. 08

HOW

- ▶ SVM-Ranking
- ▶ Stochastic optimization

Joachims 05; Usunier et al. 08, 09

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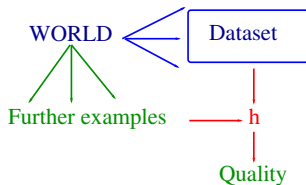
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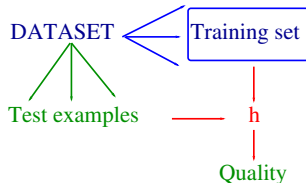
- Estimating an indicator

Validation, principle

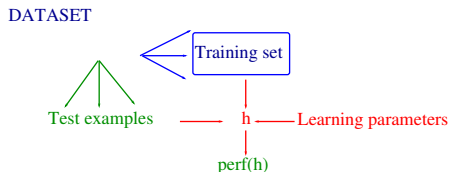
Desired: performance on further instances



Assumption: Dataset is to World, like Training set is to Dataset.



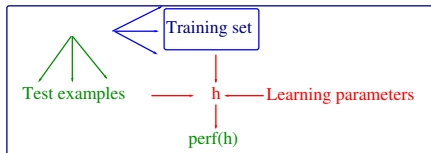
Validation, 2



Unbiased Assessment of Learning Algorithms
T. Scheffer and R. Herbrich, 97

Validation, 2

DATASET

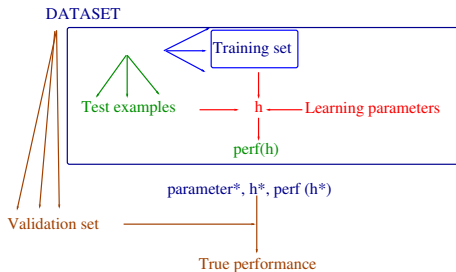


parameter*, h^* , $\text{perf}(h^*)$

Unbiased Assessment of Learning Algorithms

T. Scheffer and R. Herbrich, 97

Validation, 2



Unbiased Assessment of Learning Algorithms

T. Scheffer and R. Herbrich, 97

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Confidence intervals

Definition

Given a random variable X on $\mathbb{R}$, a $p\%$ -confidence interval is $I \subset \mathbb{R}$ such that

$$Pr(X \in I) > p$$

Binary variable with probability ϵ

Probability of r events out of n trials:

$$P_n(r) = \frac{n!}{r!(n-r)!} \epsilon^r (1-\epsilon)^{n-r}$$

- ▶ Mean: $n\epsilon$
- ▶ Variance: $\sigma^2 = n\epsilon(1-\epsilon)$

Gaussian approximation

$$P(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp^{-\frac{1}{2} \frac{x-\mu}{\sigma}^2}$$

Confidence intervals

Bounds on (true value, empirical value) for n trials, $n > 30$

$$Pr(|\hat{x}_n - x^*| > \underbrace{1.96}_Z \sqrt{\frac{\hat{x}_n \cdot (1 - \hat{x}_n)}{n}}) < \underbrace{.05}_\varepsilon$$

Table

| | | | | | | | |
|---------------|-----|----|------|------|------|------|------|
| z | .67 | 1. | 1.28 | 1.64 | 1.96 | 2.33 | 2.58 |
| ε | 50 | 32 | 20 | 10 | 5 | 2 | 1 |

Empirical estimates

When data abound

(MNIST)



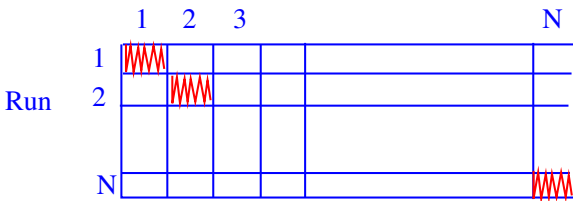
Training

Test

Validation

Cross validation

Fold

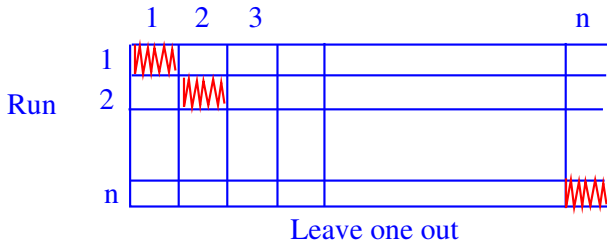


N-fold Cross Validation

Error = Average (error on  of h
learned from )

Empirical estimates, foll'd

Cross validation → Leave one out
Fold



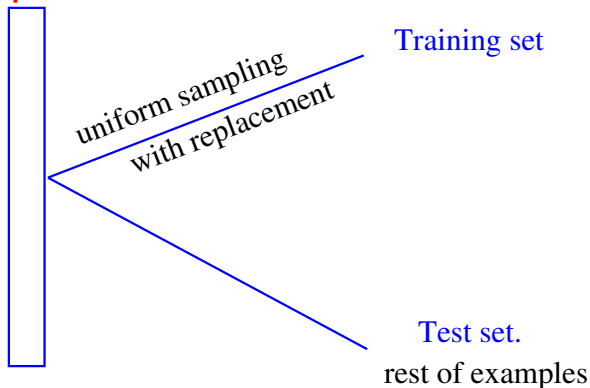
Same as N-fold CV, with $N = \text{number of examples}$.

Properties

Low bias; high variance; underestimate error if data not independent

Empirical estimates, foll'd

Bootstrap



Dataset

Average indicator over all (Training set, Test set) samplings.

Beware

Multiple hypothesis testing

- ▶ If you test many hypotheses on the same dataset
- ▶ one of them will appear confidently true...

More

- ▶ Tutorial slides:
http://www.lri.fr/~sebag/Slides/Validation_Tutorial_11.pdf
- ▶ Video and slides (soon): ICML 2012, Videolectures, Tutorial Japkowicz & Shah
<http://www.mohakshah.com/tutorials/icml2012/>

Validation, summary

What is the performance criterion

- ▶ Cost function
- ▶ Account for class imbalance
- ▶ Account for data correlations

Assessing a result

- ▶ Compute confidence intervals
- ▶ Consider baselines
- ▶ Use a validation set

If the result looks too good, don't believe it