# Data Streaming

- When: data, specificities
- What: goals
- How: algorithms

More: see Joao Gama's tutorial,

http://wiki.kdubiq.org/summerschool2008/index.php/Main/Materials

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## Motivations



Electric Power Network

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## Data

#### Input

- Continuous flow of (possibly corrupted) data, high speed
- Huge number of sensors, variable along time (failures)
- Spatio-temporal data

#### Output

- Cluster: profiles of consumers
- Prediction: peaks of demand
- Monitor Evolution: Change detection, anomaly detection

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## Where is the problem ?

Standard Data Analysis

- Select a sample
- Generate a model (clustering, neural nets, ...)

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Does not work ...

- World is not static
- Options, Users, Climate, ... change

# Specificities of data

#### Domain

- Radar: meteorological observations
- Satellite: images, radiation
- Astronomical surveys: radio
- Internet: traffic logs, user queries, ...
- Sensor networks
- Telecommunications

#### Features

- Most data never seen by humans
- Need for REAL-TIME monitoring, (intrusion, outliers, anomalies,,,)

NB: Beyond ML scope: data are not iid (independent identically distributed)

## Data streaming Challenges

#### Maintain Decision Models in real-time

incorporate new information

comply with speed

- forget old/outdated information
- detect changes and adapt models accordingly

Unbounded training sets Prefer fast approximate answers...

- Approximation: Find answer with factor  $1 \pm \epsilon$
- Probably correct:  $Pr(answer correct) = 1 \delta$
- PAC:  $\epsilon, \delta$  (Probably Approximately Correct)
- Space  $\approx \mathcal{O}(1/\epsilon^2 \log(1/\delta))$

# Data Mining vs Data Streaming

	Traditional	Stream
Nr. of Passes	Multiple	Single
Processing Time	Unlimited	Restricted
Memory Usage	Unlimited	Restricted
Type of Result	Accurate	Approximate
Distributed	No	Yes

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#### What: queries on a data stream

#### Sample

- Count number of distinct values / attribute
- Estimate sliding average (number of 1's in a sliding window)
- Get top-k elements

Application: Compute entropy of the stream

$$H(x) = \sum p_i \log_2(p_i)$$

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useful to detect anomalies

# Sampling

Uniform sampling: each one out of n examples is sampled with probability 1/n. What if we don't know the size ? Standard

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- Sample instances at periodic time intervals
- Loss of information

#### Reservoir Sampling

- Create buffer size k
- Insert first k elements
- Insert *i*-th element with probability k/i
- Delete a buffer element at random

Limitations

- Unlikely to detect changes/anomalies
- Hard to parallelize

## Count number of values

#### Problem

Domain of the attribute is  $\{1, \ldots, M\}$ Piece of cake if memory available... What if the memory available is log(M)? Flajolet-Martin 1983 Paged on backing:  $\{1, \ldots, M\}$  is  $\{0, \ldots, 2h\}$  with l = log(M)

Based on hashing:  $\{1, \ldots, M\} \mapsto \{0, \ldots, 2^L\}$  with L = log(M).

 $x \rightarrow hash(x) = y \rightarrow position least significant bit, lsb(x)$ 

## Count number of values, followed



Result

$$R = \text{ position of rightmost 0 in } H$$
  
 $M \approx 2^R / .7735$ 

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## Decision Trees for Data Streaming

#### Principle

Grow the tree if evidence best attribute > second best

#### Algorithm

parameter: confidence  $\delta$  (user-defined)

While true

Read example, propagate until a leaf

If enough examples in leaf

Compute IG for all attributes;

 $\begin{aligned} \epsilon &= \sqrt{\frac{R^2 \ln(1/\delta)}{2n}} \\ \text{Keep best if IG(best) - IG(second best }) > \epsilon \end{aligned}$ 

Mining High Speed Data Streams, Pedro Domingos, Geoffrey Hulten, KDD-00



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# Model OO Reservoir

Does  $e_t$  fit the current model ??

- ▶ if yes, update the model
- otherwise, put outlier  $e_t$  in reservoir



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Reservoir

Model OO

Has the distribution changed ?

- ▶ if yes, rebuild the model
- otherwise, continue

CHANGE TEST

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Model OO  $\bigtriangleup$ 

Reservoir

Has the distribution changed ?

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#### CHANGE TEST

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# Strap



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Does  $e_t$  fit the current model ?

- if yes, update the model
- otherwise, put e<sub>t</sub> in reservoir

Has the distribution changed ?

- if yes, rebuild the model
- otherwise, continue

#### Update the model

Stream Model:  $\{(e_i, n_i, \Sigma_i, t_i)\}$ 

e; examplar

- *n<sub>i</sub>* number of items represented by *e<sub>i</sub>*
- $\triangleright$   $\Sigma_i$  sum of distortions incurred by  $e_i$
- ▶ *t<sub>i</sub>* last time step when a point was affected to *e<sub>i</sub>*

Update with decay:

 $\Delta$ : time window

$$n_i := n_i \times \left(\frac{\Delta}{\Delta + (t - t_i)} + \frac{1}{n_i + 1}\right)$$
  

$$\Sigma_i := \Sigma_i \times \frac{\Delta}{\Delta + (t - t_i)} + \frac{n_i}{n_i + 1} d(e_t, e_i)^2$$
  

$$t_i := t$$

# Rebuild the model

#### Trigger

- when reservoir is full
- when changes are detected

Page-Hinkley statistic



$$\begin{split} \bar{p}_t &= \frac{1}{t} \sum_{\ell=1}^t p_\ell \\ m_t &= \sum_{\ell=1}^t \left( p_\ell - \bar{p}_\ell + \delta \right) \\ PH_t &= max\{m_\ell\} - m_t \end{split}$$

HINKLEY D. Inference about the change-point in a sequence of random variables. Biometrika, 1970 PAGE E. Continuous inspection schemes. Biometrika, 1954

## Experimental validation

#### Data used

- Artificial dataset
- Real world data: KDD99 data
  - intrusion detection benchmark
  - ▶ 494,021 network connection records in  $\mathbb{R}^{34}$
  - 23 classes: 1 normal + 22 attacks
- Baseline: DenStream

F. Cao, M. Ester, W. Qian, A. Zhou. Density-Based Clustering over an Evolving Data Stream with Noise. SDM 2006.

#### Performance indicator

- Distortion
- Clustering accuracy / Clustering purity (supervised setting)

KDD Cup 1999 data: http://kdd.ics.uci.edu/databases/kddcup99/kddcup99.html.

## Accuracy along time





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## Restart criteria: MaxSizeR vs PH





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## Discussion

#### Rebuild: ReservoirSize vs PH

- ▶ PH is 10% better than ReservoirSize
- PH is less stable

#### Strap vs DenStream

- Pros
  - better accuracy
  - model available at any time

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- Cons
  - DenStream: 7 seconds
  - Strap : 7 mins

## Conclusion

#### Scalability: Hi-WAP

- Reduce complexity from  $\mathcal{O}(N^2)$  to  $\mathcal{O}(N^{3/2})$
- iteratively reduce toward  $\mathcal{O}(N^{(1+\gamma)})$

#### Stream clustering: Strap

- Hybridized with an efficient change detection method, Page-Hinkley
- Model available at any time
- BUT: slower than DenStream

Future work Provide an upper bound on the distortion loss caused by Hi-WAP

## Open issues

#### What's new

Forget about iid;

Forget about more than linear complexity (and log space)

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#### Challenges

Online, Anytime algs Distributed alg. Criteria of performance Integration of change detection