Lecture 5
Significance tests
Criticisms of the NHST
Publication bias
Research planning

Theophanis Tsandilas
Calculating $p$

The $p$ value is the probability of obtaining a statistic as extreme or more extreme than the one observed if the null hypothesis was true.

When data are sampled from a known distribution, an exact $p$ can be calculated.

If the distribution is unknown, it may be possible to estimate $p$. 
Normal distributions

If the sampling distribution of the statistic is normal, we will use the standard normal distribution $z$ to derive the $p$ value.
Example

An experiment studies the IQ scores of people lacking enough sleep.

\[ H_0: \mu = 100 \text{ and } H_1: \mu < 100 \text{ (one-sided)} \]

or

\[ H_0: \mu = 100 \text{ and } H_1: \mu \neq 100 \text{ (two-sided)} \]
Example

Results from a sample of 15 participants are as follows:

90, 91, 93, 100, 101, 88, 98, 100, 87, 83, 97, 105, 99, 91, 81

The mean IQ score of the above sample is $M = 93.6$.

Is this value statistically significantly different than 100?
Creating the test statistic

We assume that the population standard deviation is known and equal to $SD = 15$. Then, the standard error of the mean is:

$$
\sigma_{\hat{\mu}} = \frac{\sigma}{\sqrt{n}} = \frac{15}{\sqrt{15}} = 3.88
$$
Creating the test statistic

We assume that the population standard deviation is known and equal to SD = 15. Then, the standard error of the mean is:

\[ \sigma_{\hat{\mu}} = \frac{\sigma}{\sqrt{n}} = \frac{15}{\sqrt{15}} = 3.88 \]

The test statistic tests the standardized difference between the observed mean \( \hat{\mu} = 93.6 \) and \( \mu_0 = 100 \)

\[ z = \frac{\hat{\mu} - \mu_0}{\sigma_{\hat{\mu}}} = \frac{93.6 - 100}{3.88} = -1.65 \]

The \( p \) value is the probability of getting a \( z \) statistic as or more extreme than this value (given that \( H_0 \) is true)
Calculating the p value

The p value is the probability of getting a z statistic as or more extreme than this value (given that H₀ is true).

$$z = \frac{\hat{\mu} - \mu_0}{\sigma_{\hat{\mu}}} = \frac{93.6 - 100}{3.88} = -1.65$$
Calculating the p value

To calculate the area in the distribution, we will work with the cumulative density probability function (cdf).

\[
\text{pnorm}(x)
\]

one sided p = .049

two sided p = .098
m0 <- 100 # mean for null hypothesis
sd <- 15 # We assume that the population sd is known

# These are the observed IQ scores
scores <- c(90, 91, 93, 100, 101, 88, 98, 100, 87, 83, 97, 105, 99, 91, 81)
m <- mean(scores)

# I calculate the standard error of the mean
se <- sd / sqrt(length(scores))

# I calculate the z statistic, i.e., the standardized mean difference
z = (m - m0) / se

# This is the one side p value
pvalue <- pnorm(z)

cat("one sided p-value =", pvalue, "\n")
cat("two sided p-value =", 2*pvalue, "\n")
Example: conclusions

If we assume that the standard deviation of the population is known (SD = 15):

We reject the null hypothesis ($\alpha = .05$) if we apply a one-sided significance test ($p = .049$).

But we cannot reject it if we apply a two-sided significance test ($p = .092$).
One-sided vs. two sided

“A common misunderstanding of directional testing is to believe that it should be employed whenever a researcher predicts an effect in a particular direction.

This is almost always bad practice. A one-sided test should be employed only if the direction of an effect is already known or if any outcome in the non-predicted direction would be ignored.

The crucial question is not whether you think an effect lies in a particular direction, but whether you are willing to declare an effect in the wrong direction non-significant (no matter how interesting or how important it is). The answer to such a question is usually ‘no’ and for this reason one-sided tests should typically be avoided.“

from Baguley
**t tests**

If the population variance is unknown and \( n \) is small, it is better to work with the \( t \) distribution.
One sample $t$

$H_0 : \mu = \mu_0$

$H_1 : \mu \neq \mu_0$

$t = \frac{\hat{\mu} - \mu_0}{\hat{\sigma} \hat{\mu}} = \frac{\hat{\mu} - \mu_0}{\hat{\sigma}/\sqrt{n}}$

Where $\hat{\sigma}$ is the unbiased estimate of the population standard deviation.

And $t$ follows a $t$ distribution with $\nu = n - 1$ degrees of freedom.
Back to our example

Results from a sample of 15 participants are as follows:

90, 91, 93, 100, 101, 88, 98, 100, 87, 83, 97, 105, 99, 91, 81

The mean IQ score of the above sample is $M = 93.6$. Is this value statistically significantly different than 100?

Assume now that we don’t have any prior knowledge of the population standard deviation.
m0 <- 100  # mean for null hypothesis

# These are the observed IQ scores
scores <- c(90, 91, 93, 100, 101, 88, 98, 100, 87, 83, 97, 105, 99, 91, 81)
n <- length(scores)
m <- mean(scores)

# I estimate the standard error of the mean
se <- sd(scores) / sqrt(n)

# I calculate the t statistic, i.e., the standardized mean difference
t = (m - m0) / se

# This is the two-sided p value, calculated from the cumulative density function of the t distribution
pvalue <- 2*pt(t, n - 1)
cat("two sided p-value =", pvalue, "\n")
R code

Alternatively, you can use the t-test function of R:

```r
> t.test(scores - 100)

One Sample t-test

data:  scores - 100
t = -3.5064, df = 14, p-value = 0.00349
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
  -10.314708  -2.485292
sample estimates:
  mean of x
  -6.4
```
Calculating the p value (two-sided)

\[ t = \frac{\hat{\mu} - \mu_0}{\hat{\sigma}_{\hat{\mu}}} = -3.5064 \]
Example: summarizing the result

\[ t(14) = -3.51, \ p = .003 \]

The researchers reject the null hypothesis. They found that the lack of sleep leads to a mean IQ score that is statistically significantly lower than 100.
p values vs. confidence intervals

2.5% of random means

95% CI

observed mean

μ̄

μ₀

-μ

2.5% of random means

p = .05
p values vs. confidence intervals

$\mu_0 \quad \mu \quad -\mu \\
1.8\% \text{ of random means} \\
95\% \text{ CI}

p = .036

means of random samples from a null distribution

1.8\% \text{ of random means}
p values vs. confidence intervals

\[ p = 0.086 \]

\[ \mu \]

\[ \mu_0 \]

\[ -\mu \]

4.3% of random means

95% CI

observed mean

means of random samples from a null distribution

4.3% of random means
Independent $t$ test

NHST of a difference between the means of two independent normal samples.

$H_0 : \mu_1 = \mu_2$

$H_1 : \mu_1 \neq \mu_2$

$$t = \frac{\hat{\mu}_1 - \hat{\mu}_2}{\hat{\sigma}_{\hat{\mu}_1 - \hat{\mu}_2}} \sim t(\nu)$$

If we assume equal variances, then:

$$\nu = (n_1 + n_2) - 2 \quad \text{and} \quad \hat{\sigma}_{\hat{\mu}_1 - \hat{\mu}_2} = \hat{\sigma}_{\text{pooled}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$
Independent $t$ test

NHST of a difference between the means of two independent normal samples.

$$H_0 : \mu_1 = \mu_2$$

$$H_1 : \mu_1 \neq \mu_2$$

$$t = \frac{\hat{\mu}_1 - \hat{\mu}_2}{\hat{\sigma}_{\hat{\mu}_1-\hat{\mu}_2}} \sim t(\nu)$$

But if variances are unequal, the Welch-Satterthwaite correction should be used. Please, check the slides of Lecture 3 for more details.
Example

A research team is interested in comparing the performance in an IQ test between two groups: adults who have (G1) and adults who have not (G2) completed any graduate studies.

From each group, they test 15 participants.


$S_{G2}: 96, 108, 90, 104, 97, 103, 95, 102, 93, 107, 101, 88, 99, 104, 97$
R code

```r
> scores2 <- c(96, 108, 90, 104, 97, 103, 95, 102, 93, 107, 101, 88, 99, 104, 97)
> t.test(scores1, scores2)

Welch Two Sample t-test

data:  scores1 and scores2
t = 2.9411, df = 27.316, p-value = 0.006589
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
  1.796244 10.070423
sample estimates:
mean of x mean of y
104.86667 98.93333
```

Corrected for unequal variances by default
Example: summarizing the results

\[ t(27.32) = 2.94, \ p = .007 \]

The researchers reject the null hypothesis (\( \alpha = .05 \)).

They conclude that the mean IQ score of adults who have completed graduate studies (G1) is statistically significantly higher than the IQ score of adults who have not completed any graduate studies (G2).
Example: summarizing the results

The 95% confidence intervals for this same example.
Paired observations

A research team is interested in comparing the performance in an IQ test before and after attending a Geometry course:

10 participants are tested before and after the completion of the course.

$S_{Before}: 102, 94, 90, 104, 95, 100, 101, 96, 100, 96$

$S_{After}: 106, 108, 93, 103, 100, 100, 105, 98, 103, 96$
Paired $t$ test

The solution is again trivial. We calculate the difference in performance for each participant.

<table>
<thead>
<tr>
<th></th>
<th>P1</th>
<th>P2</th>
<th>P3</th>
<th>P4</th>
<th>P5</th>
<th>P6</th>
<th>P7</th>
<th>P8</th>
<th>P9</th>
<th>P10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Before</td>
<td>102</td>
<td>94</td>
<td>90</td>
<td>104</td>
<td>95</td>
<td>100</td>
<td>101</td>
<td>96</td>
<td>100</td>
<td>96</td>
</tr>
<tr>
<td>After</td>
<td>106</td>
<td>108</td>
<td>93</td>
<td>103</td>
<td>100</td>
<td>100</td>
<td>105</td>
<td>98</td>
<td>103</td>
<td>96</td>
</tr>
<tr>
<td>Diff.</td>
<td>4</td>
<td>14</td>
<td>3</td>
<td>-1</td>
<td>5</td>
<td>0</td>
<td>4</td>
<td>2</td>
<td>3</td>
<td>0</td>
</tr>
</tbody>
</table>

and then perform the one sample $t$ test on these differences.
R code

```r
> scores.before <- c(102, 94, 90, 104, 95, 100, 101, 96, 100, 96)
> scores.after <- c(106, 108, 93, 103, 100, 100, 105, 98, 103, 96)
> t.test(scores.after - scores.before)

One Sample t-test

data:  scores.after - scores.before

  t = 2.5468, df = 9, p-value = 0.03136
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
  0.3800225 6.4199775
sample estimates:
  mean of x
          3.4

> t.test(scores.after, scores.before, paired = TRUE)

Paired t-test

data:  scores.after and scores.before

  t = 2.5468, df = 9, p-value = 0.03136
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
  0.3800225 6.4199775
sample estimates:
  mean of the differences
          3.4
```
Lognormal distributions

We follow the same approach as for confidence intervals:

We simply apply the t tests on the logarithms of the original values and reject the null hypothesis if $p < \alpha$. 
Reporting results of statistical tests

APA’s (American Psychology Association) style:

Report the exact $p$ value within the test (unless the $p$ value is less than .001)

$t(7) = 1.92, p = .022$
$t(54) = 5.43, p < .001$
$t(19) = -0.75, p = .460$

Two decimal points

See: http://my.ilstu.edu/~jhkahn/apastats.html

In other research disciplines, lower thresholds may be used.
Reporting results of statistical tests

The Statistical American Association (ASA) recommends reporting precise \textit{p-values}: \url{https://amstat.tandfonline.com/doi/suppl/10.1080/00031305.2016.1154108?scroll=top#.XEB0js9Kj0A}

However, it is not clear whether it makes sense to report very small \textit{p}-values (e.g., lower than .0001) in disciplines that deal with small amounts of data, and statistical assumptions may not be very accurate.

A good practice may be to report precise values while being careful about their interpretation. An extremely small \textit{p}-value (e.g., .00000001) may not necessarily provide stronger statistical evidence than a larger \textit{p}-value (e.g., .001), in particular when data are messy, samples are not large, and statistical assumptions are not accurate.
Type I error

Incorrectly rejecting the null hypothesis (false positive)

Type I error rate = the probability of rejecting the null hypothesis given that it is true.

When $\alpha = .05$, one expects that the Type I error rate of a significance test is 5%.
Type II error

Failing to reject the null hypothesis when it is not true (false negative)

Type II error rate = the probability of failing to reject the null hypothesis given that it is not true

The Type II error rate is often denoted as $\beta$ (beta)
Controlling for the Type II error rate

Significance tests do not provide any guarantee for the Type II error rate.

The larger the size of the sample, the lower the Type II error rate is expected to be.

It also depends on how large or small the effect of interest (such as the difference between two means) is.
Assessing Type II error rates with R

N <- 10000 # Number of experiments
m0 <- 100 # mean of null distribution

# population mean and standard deviation
m = 90
sd = 15

n <- 20 # Sample size

alpha <- .05 # Significance (alpha) level
typeII.errors <- 0

for(i in 1:N){
    sample <- rnorm(n, m, sd)
    p <- t.test(sample - m0)$p.value
    if(p > alpha) typeII.errors <- typeII.errors + 1
}

cat("Type II error rate:", typeII.errors / N, "\n")

These values will determine the Type II error rate.
Statistical power

It is defined as follows:

\[
\text{power} = \Pr(\text{reject } H_0 \mid H_1 \text{ is true}) = 1 - \beta
\]

**Example:** If the Type II error rate is \( \beta = .3 \), then the power is \( 1 - .3 = .7 \) or 70%.

We say that a study has high statistical power, if it is expected to reject the null hypothesis \((H_0)\) with a high probability, given that \(H_1\) is true.
Predicting the power of an experiment

1: Assess the minimum expected **effect size** of interest
   How small are the differences that we want to be able to show?

2: Assess the variance in the population of interest.
   (This may not be easy)

3: Based on the above parameters, estimate the minimum sample size needed to show the effect of interest.
   Small differences and large variance require larger sample sizes
Underpowered studies

Such studies are unlikely to allow the researcher to choose between $H_0$ and $H_1$ at the desired significance level (e.g., $\alpha = .05$). They have high Type II error rates.
Underpowered studies

Main reasons for low statistical power:

- Inadequate sample sizes. This is a common problem for many research disciplines (including HCI research).

- Failure to identify potential sources of noise or variance and well control the experimental task. This is always a challenge for researchers.

- Large measurement error. A good choice of measures and measurements over multiple task replications could reduce this problem
Reducing sources of variance

Provide clear experimental instructions that are consistent across participants.

If learning effects are not of interest, provide enough training before the main experiment.

Avoid long sessions to minimize fatigue effects.

Carefully design the experiment through pilot studies.
Pilot studies (pilot experiments)

Informal small-scale preliminary studies conducted prior to a formal full-scale study:

• Assess the feasibility, time and cost of a study

• Identify problems (e.g., adverse effects) and refine the experimental procedures

• Predict how large or small the effect of interest is

  Example: How large or small do we expect the difference in IQ scores between two different groups to be?

• Predict the appropriate sample size for the formal study to ensure adequate statistical power.
What is a reasonable power level?

A power of 80% is generally considered as a good level of power. (Type II Error rate = .20)

Compare this with the 95% confidence level that we commonly use (Type I Error rate = .05)
Type I vs. Type II error

Some reasonable questions:

Q1. Why do we allow any errors at all?

Q2. Why are we mostly concerned about Type I errors (false positives) and less about Type II errors (false negatives)?

Note: The discussion in the following slides is based on Toby Mordkoff’s course notes: http://www2.psychology.uiowa.edu/faculty/mordkoff/GradStats/part%201/I.13%2012power.pdf
Q1. Why allowing errors?

It is a necessity!

As the normal distribution goes to infinity in both directions, the bounds of 100% confidence intervals are always $[-\infty, \infty]$.

Such confidence intervals are non-informative and useless.

Similarly, if we wanted to eliminate Type I errors ($\alpha = 0$), we would never be able to reject the null hypothesis.
Q2. Why does science focus on Type I errors?

By tradition, science is conservative:

By default, it assumes a no effect until someone shows an effect (i.e., rejects the null hypothesis).

Failure to reject the null hypothesis does not change our understanding of reality.

In contrast, rejecting a null hypothesis changes this understanding. If such rejection is false (Type I error), then the cost can be high.
Publication bias

Priority is traditionally given to papers that report on positive results (i.e., ones that confirm an effect).

Why? Because anybody can run a lousy, underpowered experiment (e.g., one that does not try to reduce variance) or an experiment on non-effective treatments or techniques that fails to reject the null hypothesis.

Research disciplines try to protected themselves from the influence of lousy experiments. By not publishing such results, they reduce the influence of Type II errors.
Example

Imagine a drug company that advertises the results of some published studies:

“nothing has been shown to work better”
“no side effects above those with placebo”

Both results may be due to Type II errors.

How difficult do you think it is to produce such results?

Note: Based on Toby Mordkoff’s course notes: http://www2.psychology.uiowa.edu/faculty/mordkoff/GradStats/part%201/1.13%2012power.pdf
Dangers of publication bias (1)

**But:** By not publishing negative results, the influence of Type I errors can become great.
Example: Telepathy

An experiment studies whether two remote people (a sender and a receiver) can communicate information without any physical interaction.

The sender picks a card with a random number from 1 to 5 and tries to communicate it to the receiver. The receiver tries to guess the number communicated by the sender.

$H_0$: The receiver has a 20% chance to guess the correct number.

$H_1$: The receiver guesses the correct number with a rate that is higher than chance (20%).
Example: Telepathy

Imagine that different parapsychologists conduct this same experiment many times. The graph below shows the 95% CI of 14 different experiments.
Example: Telepathy

Imagine that different parapsychologists conduct this same experiment many times. The graph below shows the 95% CI of 14 different experiments.

For these studies, the researchers abandon their efforts. They do not even try to publish their results.
Example: Telepathy

Imagine that different parapsychologists conduct this same experiment many times. The graph below shows the 95% CI of 14 different experiments.

The researchers submit their results for publication. But all these papers are rejected.
Example: Telepathy

Imagine that different parapsychologists conduct this same experiment many times. The graph below shows the 95% CI of 14 different experiments.

These researchers celebrate! They are the first to provide statistical evidence on the existence of telepathy. A journal accepts their paper. Their results appear on the headlines of mainstream press and trigger many discussions in the social media.
The importance of replication

Such results can be put into question by replicating the experiment. Thus, **publishing the results of replication studies can be important, even if those results are negative.**

In several disciplines, replication is a common practice. Conclusions are often based on **meta-analyses** of the results of several independent studies.

Unfortunately, in other disciplines (e.g., in HCI), replications are rare exceptions.
Effects of remote, retroactive intercessory prayer on outcomes in patients with bloodstream infection: randomised controlled trial

*BMJ* 2001; 323 doi: https://doi.org/10.1136/bmj.323.7327.1450 (Published 22 December 2001)

**Subjects:** All 3393 adult patients whose bloodstream infection was detected at the hospital in 1990-6.

**Intervention:** In July 2000 patients were randomised to a control group and an intervention group. A remote, retroactive intercessory prayer was said for the well being and full recovery of the intervention group.

**Main outcome measures:** Mortality in hospital, length of stay in hospital, and duration of fever.

**Results:** Mortality was 28.1% (475/1691) in the intervention group and 30.2% (514/1702) in the control group (P for difference=0.4). Length of stay in hospital and duration of fever were significantly shorter in the intervention group than in the control group (P=0.01 and P=0.04, respectively).

**Conclusions:** Remote, retroactive intercessory prayer said for a group is associated with a shorter stay in hospital and shorter duration of fever in patients with a bloodstream infection and should be considered for use in clinical practice.
This study is clearly flawed! The author here has just divided (by chance or intentionally) the control and the intervention group in a convenient way. It is trivial to show the flaw!

Create a script that randomly divides the patients into two groups (control vs. intervention). Repeat it 1000 times. Each time, pray for the intervention group!

For approximately 50 of these repetitions, you will be able to reject the null hypothesis, i.e., you will find that retroactive prayer works!
Over half of psychology studies fail reproducibility test

Largest replication study to date casts doubt on many published positive results.

Monya Baker

27 August 2015

Don't trust everything you read in the psychology literature. In fact, two thirds of it should probably be distrusted.

In the biggest project of its kind, Brian Nosek, a social psychologist and head of the Center for Open Science in Charlottesville, Virginia, and 269 co-authors repeated work reported in 98 original papers from three psychology journals, to see if they independently came up with the same results.
Dangers of publication bias (2)

Reaching statistical significance \((p < .05)\) has somehow become the ultimate goal of research.

This has also lead to **misuses of significance tests** and unscientific but widely spread practices, commonly known as **p hacking**.
Common $p$-hacking techniques

Incrementally increase the sample size $n$ (by recruiting new participants) until statistical significance is achieved.

Selectively remove “outliers” or replace participants that do not conform to the expectations of researchers.

Change the goals or hypotheses based on the results. A common practice is to focus on random “statistically significant” results, even if these results were not part of the initial experimental goals.

Apply different significance tests and pick the one that leads to significance, often disregarding its underlying assumptions.
*p* hacking and Type I error

Write an R simulation that estimates the Type I error of a simple *t* test when incrementally increasing the sample size of an experiment.
R Code

N <- 10000 # Number of experiments
n <- 12 # Initial sample size
nmax <- 16 # Max sample size. Here, the researcher stops the experiment.

alpha <- .05

error <- 0
for(i in 1:N){
  count <- n
  sample <- rnorm(n)
  p <- t.test(sample)$p.value

  while(p > alpha && count <= nmax){
    sample <- c(sample, rnorm(1))
    p <- t.test(sample)$p.value
    count <- count + 1
  }

  if(p < alpha) error <- error + 1
}

cat("Type I error:", error / N, "\n")
Multiverse Analyses: Report on the results of multiple alternative statistical analyses

https://explorablemultiverse.github.io/

With **explorable multiverse analysis reports**, readers of research papers can explore alternative analysis options by interacting with the paper itself. This new approach to statistical reporting draws from two recent ideas: multiverse analysis, a philosophy of statistical reporting where paper authors report the outcomes of many different statistical analyses in order to show how fragile or robust their findings are; and **explorable explanations**, narratives that can be read as normal explanations but where the reader can also become active by dynamically changing some elements of the explanation.
Criticisms of the Null Hypothesis Significance Testing (NHST)

Many have recommended abandoning null hypothesis testing altogether and focusing on estimation based on confidence intervals, effect sizes, and meta-analyses.

Confidence intervals: Estimate the range of plausible values of a statistic.

Effect sizes: Estimate how large or small an effect is

Meta-analysis: Emphasis on replication and integration of evidence from multiple studies.
Criticisms of NHST

"We need to make two substantial changes to how we carry out research. First, in response to heightened concern that our published research literature is incomplete and untrustworthy, we need new requirements to ensure research integrity. These include **full pre-specification of studies** wherever possible, **avoidance of selection** and other inappropriate data analytic practices, **complete reporting** of research, and encouragement of **replication**. Second, renewed recognition of the many severe flaws of null hypothesis significance testing (NHST) motivates a shift from reliance on NHST to estimation. ‘The new statistics’ refers to the full range of recommended practices, including **estimation based on effect sizes (ESs), confidence intervals (CIs), and meta-analysis.**"

[Geoff Cumming, 2013]
CIs vs. $p$ values

Both are based on similar assumptions and can be used for null hypothesis testing.

However, each provides a different amount of information:

A $p$ value is only used for **dichotomous** hypothesis testing:
If $p < .05$, then $H_0$ is rejected. Otherwise, nothing can be said.

A CI provides a range of plausible values. It can be used for estimation, irrespective of whether $H_0$ is rejected or not.
CIs vs. \( p \) values

\( p \) values or 95\% CI? What is more informative here?

Given this interval, we can reasonably conclude that the difference between C and A is very likely lower than 1.

These \( p \)-values are the same and tell us very little!

Fig. 6 95\% confidence intervals showing differences between conditions.
CIs vs. $p$ values

$p$ values or 95% CI? What is more informative here?

**Fig. 4** Showing the most plausible effect sizes and their associated uncertainty using a) $p$-values with point estimates of effect sizes (here shown as bar charts); b) 95% CIs around point estimates.
CIs and prediction of future results

On average, a 95% CI will include 83.4% of future replication means (Cumming & Maillardet, 2006)

This has been shown with simulation experiments on normal distributions.

Figure 1. Means with 95% confidence intervals (CIs) for 20 independent samples (i.e., 20 replications) from a normal population. The CIs all have the same width because $\sigma$ is assumed known. The population mean $\mu = 50$ is marked by the horizontal line. In cases in which the CI does not include $\mu$, the sample mean is shown as an open circle: There is one case here, and in the long run, 5% of samples will give CIs that do not include $\mu$. In cases in which a mean does not fall within the previous CI, the sample mean is marked with a short horizontal line: There are three cases here, and in the long run, 16.6% of means will fall outside the previous CI.
American Statistical Association (ASA)

ASA’s statement on p values (2016):

1. P-values can indicate how incompatible the data are with a specified statistical model.

2. P-values do not measure the probability that the studied hypothesis is true, or the probability that the data were produced by random chance alone.

3. Scientific conclusions and business or policy decisions should not be based only on whether a p-value passes a specific threshold.

4. Proper inference requires full reporting and transparency.

5. A p-value, or statistical significance, does not measure the size of an effect or the importance of a result.

6. By itself, a p-value does not provide a good measure of evidence regarding a model or hypothesis.

Full statement:
Interview with ASA’s executive director

Ron Wasserstein:

In the post p<0.05 era, scientific argumentation is not based on whether a p-value is small enough or not. Attention is paid to effect sizes and confidence intervals. Evidence is thought of as being continuous rather than some sort of dichotomy. (As a start to that thinking, if p-values are reported, we would see their numeric value rather than an inequality (p=.0168 rather than p<0.05)). All of the assumptions made that contribute information to inference should be examined, including the choices made regarding which data is analyzed and how. In the post p<0.05 era, sound statistical analysis will still be important, but no single numerical value, and certainly not the p-value, will substitute for thoughtful statistical and scientific reasoning.

March 2016

Interview text: http://retractionwatch.com/2016/03/07/were-using-a-common-statistical-test-all-wrong-statisticians-want-to-fix-that/
Why then still using $p$ values?

“More drastic steps, such as the ban on publishing papers that contain $P$ values instituted by at least one journal, could be counter-productive, says Andrew Vickers, a biostatistician at Memorial Sloan Kettering Cancer Center in New York City.

He compares attempts to ban the use of $P$ values to addressing the risk of automobile accidents by warning people not to drive - a message that many in the target audience would probably ignore. Instead, Vickers says that researchers should be instructed to treat statistics as a science, and not a recipe.”

http://www.nature.com/news/statisticians-issue-warning-over-misuse-of-p-values-1.19503
Why then still using $p$ values?

"One reason for its continued use is the lack of an agreed alternative. At this stage, it is sufficient to realize that statistical significance is only one, relatively modest, component in the evaluation of quantitative data.

This point has been articulated by a number of experts, notably by Abelson (1995). Abelson’s position is that statistics can be viewed as a form of principled argument. Statistical significance, in the form of a conventional NHST, is only one potential element of such an argument."

[Thom Baguley]
Why then still using $p$ values?

"The main drawback of making the switch to CIs is that it can be difficult to translate some tests into equivalent interval estimates that are both easy to interpret and easy to plot (e.g., tests with multiple degrees of freedom). These situations provide the strongest case for retaining NHSTs."

[Thom Baguley]
Different approaches

Some advise abandoning NHST and p-values

Others give a priority to estimation through confidence intervals but often use them in combination with NHST, depending on each particular case.

Others have turned to alternative statistical methods, such as **Likelihood ratios** and **Bayesian statistics** (which have their own difficulties and limitations — in particular, they are not well known in some research domains)
2. Don’t Say “Statistically Significant”

The ASA Statement on P-Values and Statistical Significance stopped just short of recommending that declarations of “statistical significance” be abandoned. We take that step here. We conclude, based on our review of the articles in this special issue and the broader literature, that it is time to stop using the term “statistically significant” entirely. Nor should variants such as “significantly different,” “p < 0.05,” and “nonsignificant” survive, whether expressed in words, by asterisks in a table, or in some other way.
Multiple Comparisons and Registration
Example

Suppose a research team is interested in whether and how listening to music affects the performance of kids in IQ tests. To this end, they test three groups of 10 year old participants:

(G1) No music (20 participants)
(G2) Classical music (20 participants)
(G3) Rock music (20 participants)

These are the IQ scores for the three groups:

G1 <- c(102, 97, 90, 107, 89, 104, 101, 112, 86, 108, 113, 94, 80, 98, 101, 107, 103, 111, 93, 99)
G3 <- c(105, 83, 92, 106, 98, 86, 103, 87, 97, 103, 83, 90, 105, 79, 100, 96, 97, 105, 95, 99)
Summary of results

Bars show 95% Confidence Intervals

One could claim here that there is a statistically significant difference ($\alpha = .05$) between these two groups.
Summary of results

But the researchers perform a total of 3 comparisons here.

Unfortunately, the more the comparisons, the more the danger to find a random difference as statistically significant!

The Type I error rate increases with the number of tests that we do.
Accounting for multiple comparisons

We adjust the $\alpha$ level with respect to the number $k$ of comparisons that we test: $\alpha_k = \alpha / k$

For $k = 3$ comparisons and $\alpha = .05$, the corrected level will be $\alpha_3 = 0.05/3 = .0167 = 1.67\%$

Thus, a difference will be assessed as statistically significant if $p < .0167$

(This is commonly known as the Bonferroni correction)
Corrected Confidence Intervals

To account for $k$ comparisons, we will construct $(100 - \alpha/k)\%$ CIs

For example, for 3 comparisons we will correct the 95% CIs by constructing $(100 - 1.67)\% = 98.33\%$ CIs
Back to our example

Bars show 95% CIs - **RED** extensions correspond to Bonferroni corrected CIs

How clear is this difference?
Problems

There is no clear consensus on how to correct for multiple comparisons.

Should we also correct for comparisons on different independent variables?

Should we correct for planned tests whose effect has been predicted in advance or only for multiple post hoc comparisons?
Some good practices

Try to predict the effects based on previous theory, past studies, or pilot tests.

Plan the comparisons of interest in advance.

Assess the power of an experimental design and select sample sizes with respect to the number of planned comparisons.

Keep the number of comparisons low.

In contrast, conducting all possible tests, looking for all possible differences is a bad practice.
Preregistration

Many disciplines and scientific journals have started encouraging (or even requiring) the **preregistration** of research protocols.

Preregistration is a kind of publishing the goals, hypotheses, and methodology (procedures, sample sizes, types of analysis and tests, etc.) of a study before it begins.

The goal is to avoid publication bias and reduce the risk of false positive results, thus reduce the risk of Type I errors.
Preregistration

There are several open services for registering research protocols, e.g., see the Open Science Framework [https://osf.io/registries]
First analysis of ‘pre-registered’ studies shows sharp rise in null findings

Logging hypotheses and protocols before performing research seems to work as intended: to reduce publication bias for positive results.

<table>
<thead>
<tr>
<th>Hypotheses Not Supported by Research Papers (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Estimates from general literature 5–20%</td>
</tr>
<tr>
<td>Registered reports for novel studies 55%*</td>
</tr>
<tr>
<td>Registered reports for replication studies 66%*</td>
</tr>
</tbody>
</table>

*Sample size: 296 hypotheses across 113 studies in biomedicine and psychology

Exploratory Findings vs. Confirmatory Tests

There is a distinction between confirmatory research that uses data to test hypotheses and exploratory research that uses data to generate hypotheses.

Some studies can be largely exploratory, helping researchers to identify interesting patterns or trends in the data that were not evident before running the study.

Researchers should clearly distinguish between their confirmatory tests and their exploratory findings. The latter need confirmation by future studies.