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Prof. Burkhart Wolff wolff@lri.fr
www.lri.fr/~wolff/teach-material/2022-2023/M2-CSMR/

# TP 1 - Introduction to Isabelle/HOL

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## Exercice 1 (Installation)

Install Isabelle(version 2022) from the Isabelle website https://isabelle.in.tum.de. Start Isabelle and make yourself familiar with the documentation, in particular the overview "What's in Main" where "Main" is the standard HOL library we base our exercises on.

## Exercice 2 (Editing, Type-Checking, Searching)

Use the Isabelle commands, typ, term and prop to enter types, terms and propositions into the system, thus using the parser and type-checker of Isabelle.

Start an anonymous session with isabelle jedit and create an anonymous session with

theory Scratch imports Main begin

#### Questions

1. Enter, parse and type-check (if possible) some types, terms, and propositions. The result should look similar to this : Change types, terms and props at your guise though.

Scratch.thy (~/)	
9 <b>1</b>	theory Scratch
L 2	imports Main
ΘЗ	begin
4	
5	<pre>section<td1></td1></pre>
6	
7	<b>typ</b> <nat <math="">\Rightarrow nat list&gt;</nat>
8	
9	<b>term</b> $\langle \lambda x. x \rangle$
10	
11	$prop (A \implies B \implies C)$
12	

FIGURE 1 – example caption

2. Enter, parse and type-check (if possible) the term

$$(\lambda x.\lambda y.(\lambda z.(\lambda x.z \ x)(\lambda y.z \ y))(x \ y))$$

(It might be helpful to add spaces ...) Note how the system represents bound and free variables.

3. Define via a number of definitions the Church Numerals of the slides of class 1. The syntax is :

definition  $const_name$  :: typ where "eqn"

Which type do Church-Numerals have in the typed  $\lambda$ -calculus?

4. axiomatize the Y-combinator, i.e. enter "Y f = f(Y f)" as axiom into the system. The syntax is :

axiomatization  $const_name :: typ$  where  $ax_name : "eqn"$ 

Which (external) type has to be given to the Y-combinator for this axiomatization?

- 5. use find\_theorems to browse your theory so far! You will need this possibility later on !
- 6. Prove that, according to your definitions, *PLUS TWO THREE* is indeed *FIVE*. Hint : state a lemma for this equation, unfold the definitions, and apply the simplification method by simp

#### Exercice 3 (OPTIONAL : Report (IN CASE THAT YOU WANT TO HAVE IT GRADED :))

1. Write a little report answering all questions above, note the difficulties you met, add some screenshots if appropriate. 3 pages max.